

# Neutrinos in Large-scale structure

Marilena LoVerde  
University of Chicago



# Neutrinos in Large-scale structure

Marilena LoVerde  
University of Chicago

ML and Zaldarriaga 1310.6459

ML 1405.4855

ML 1404:4858

ML in prep.



# Outline

- Neutrinos
- Neutrinos in Cosmology
- Massive Neutrinos in Large-scale structure
  - Halo bias
  - Halo abundance
  - Neutrino halos
- Observational Consequences



Neutrinos



# Neutrinos

flavor eigenstates

$\nu_{\text{electron}}$

$\nu_{\text{tau}}$

$\nu_{\text{muon}}$

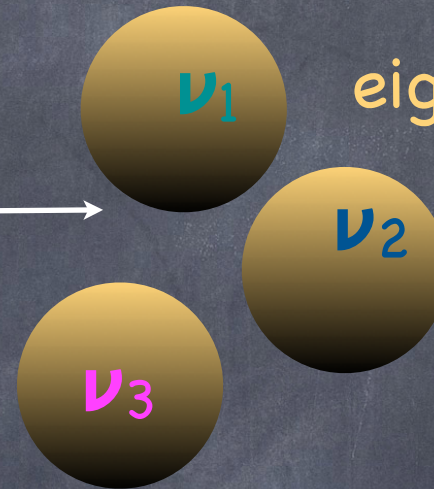


# Neutrinos

flavor eigenstates



mass eigenstates



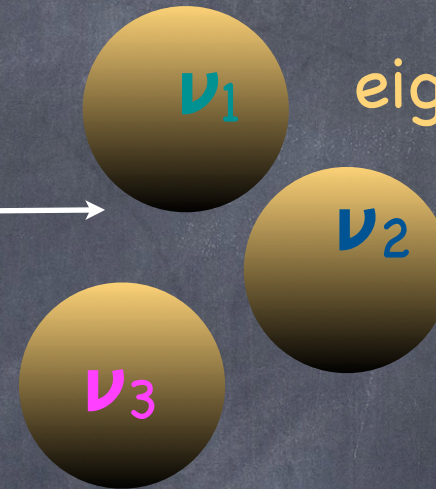


# Neutrinos

flavor eigenstates



mass eigenstates



flavor eigenstates  $\neq$  mass eigenstates

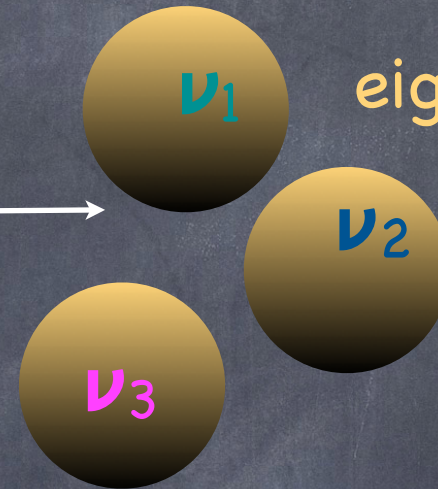


# Neutrinos

flavor eigenstates



mass eigenstates



oscillation data gives mass splittings

$$m_2^2 - m_1^2 = (7.5 \pm 0.2) 10^{-5} \text{ eV}^2 \quad (\text{solar neutrino oscillations})$$

$$|m_3^2 - m_2^2| = (2.32^{+0.12}_{-0.08}) 10^{-3} \text{ eV}^2 \quad (\text{atmospheric neutrino oscillations})$$

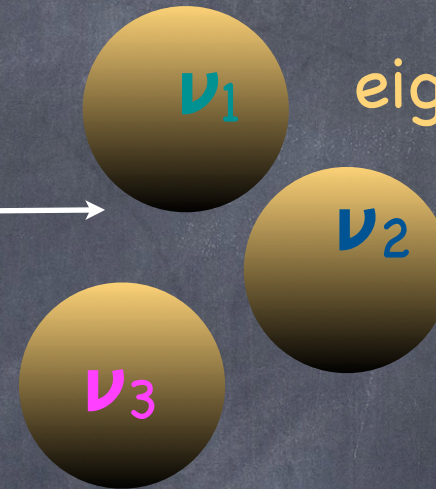


# Neutrinos

flavor eigenstates



mass eigenstates



but the absolute masses are unknown!

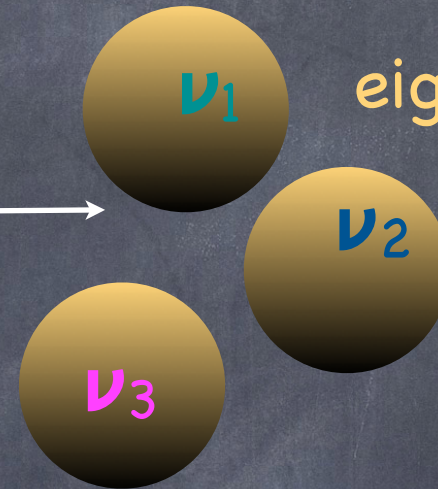


# Neutrinos

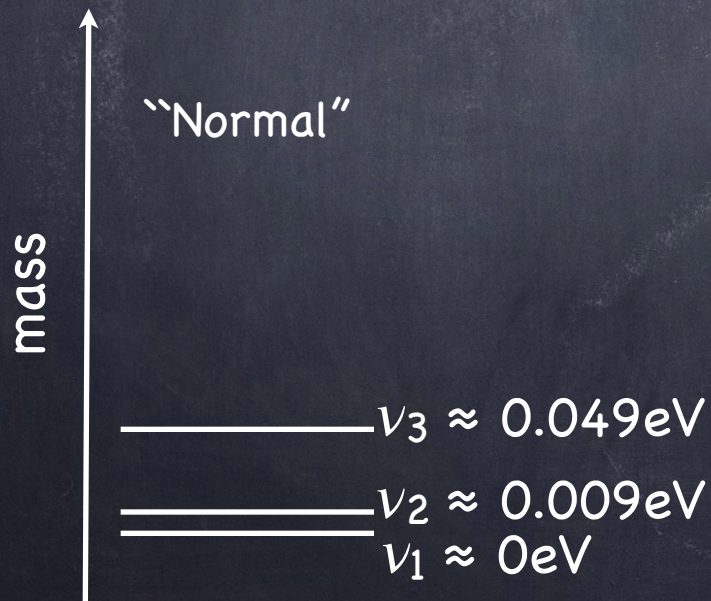
flavor eigenstates



mass eigenstates



but the absolute masses are unknown!



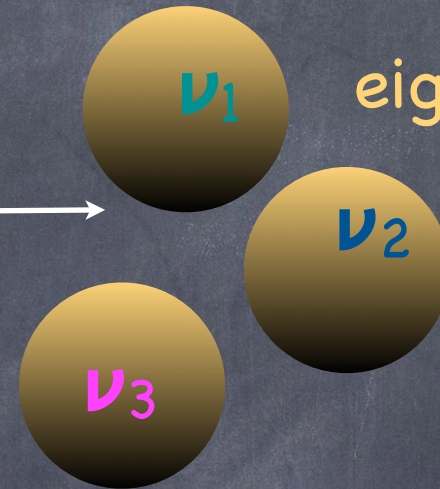


# Neutrinos

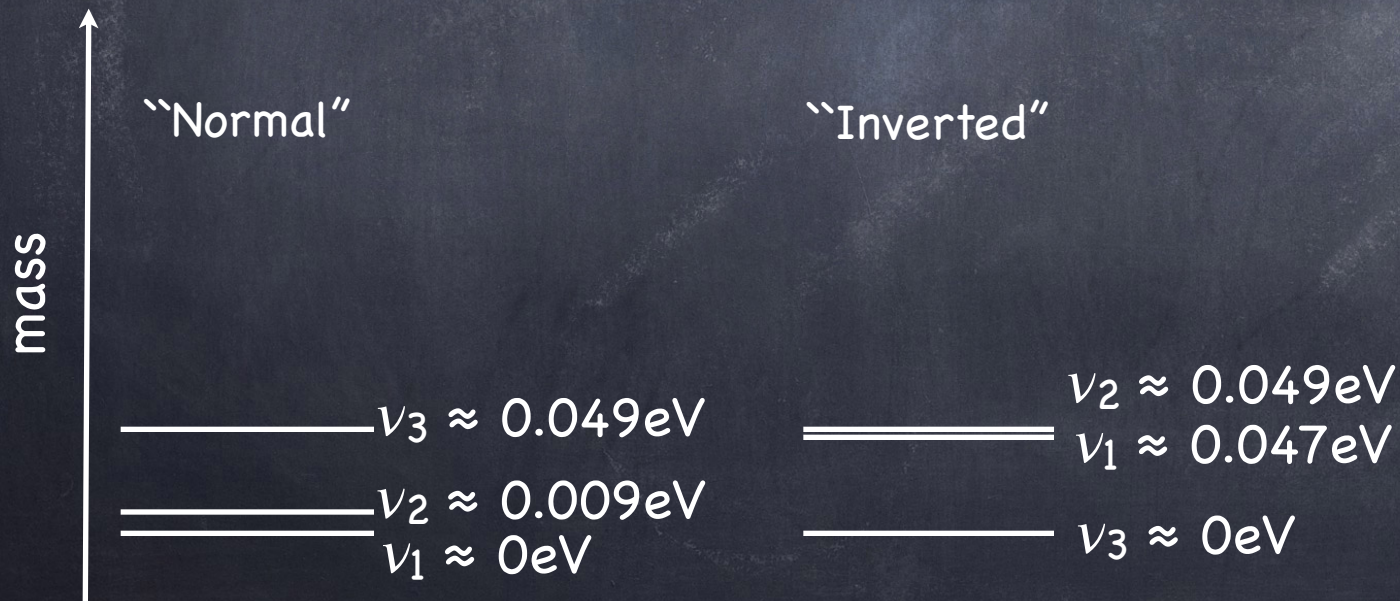
flavor eigenstates



mass eigenstates



but the absolute masses are unknown!



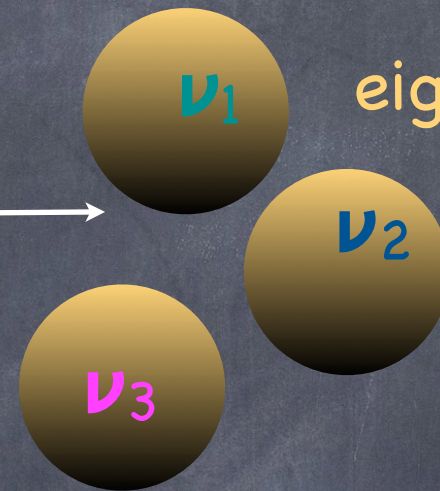


# Neutrinos

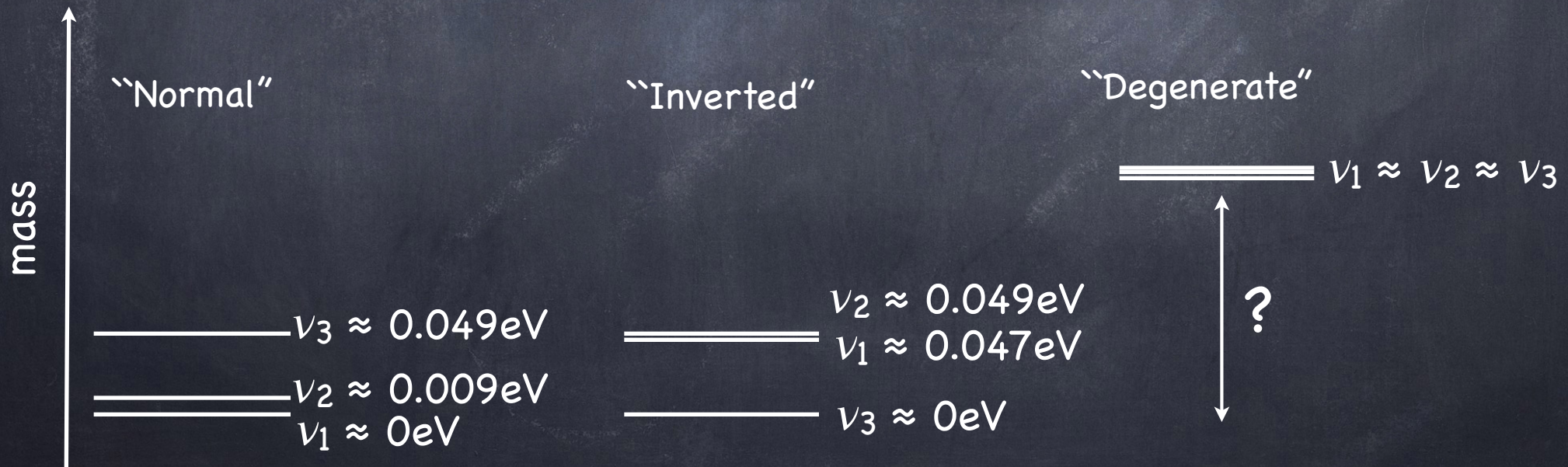
flavor eigenstates



mass eigenstates



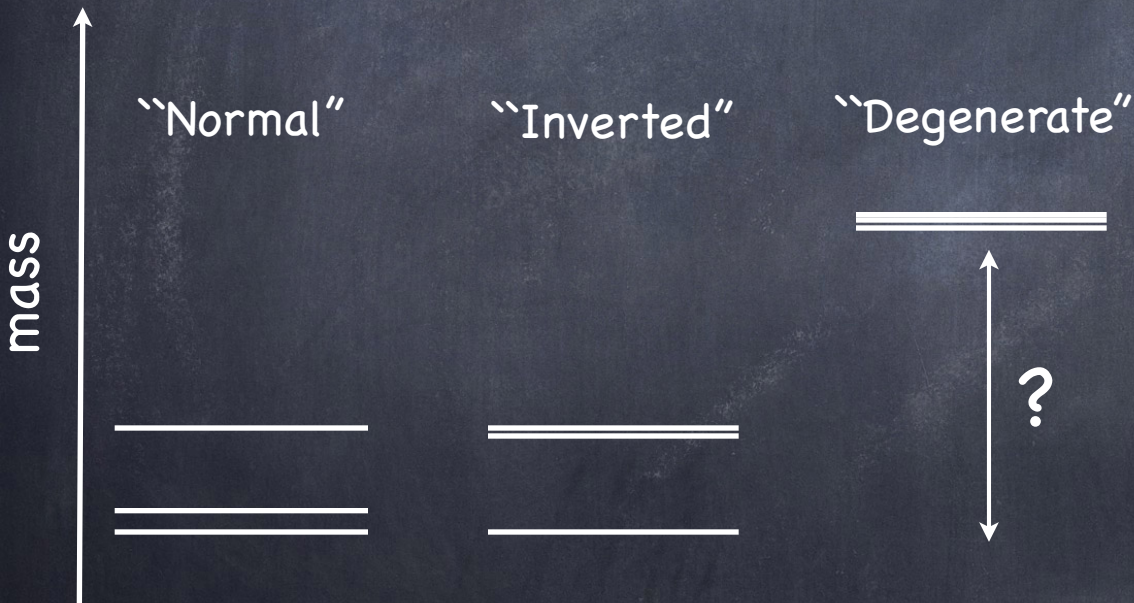
but the absolute masses are unknown!





# Neutrino knowns and unknowns

Absolute scale, hierarchy



Tritium  $\beta$  decay:  $m_{\nu\bar{e}} \lesssim 2\text{eV}$   
upper bound on mass  
(Troitsk experiment 2011)

cosmology:  $\sum m_{\nu_i} \lesssim 0.2-0.6\text{eV}$   
upper bound on mass  
(Planck CMB + BAO 2013)

$\nu_i \gtrsim 0.05\text{eV}$   
lower bound on mass  
from oscillation data



# Neutrino knowns and unknowns

## Big Questions

- Where do neutrino masses come from?
- What is the absolute mass scale?
- Are there additional sterile neutrinos?
- Can neutrinos generate matter-antimatter asymmetry of the universe?



# Neutrino knowns and unknowns

## Big Questions

- Where do neutrino masses come from?
- What is the absolute mass scale?
- Are there additional sterile neutrinos?
- Can neutrinos generate matter-antimatter asymmetry of the universe?



# Neutrino knowns and unknowns

## Big Questions

- Where do neutrino masses come from?
- What is the absolute mass scale?
- Are there additional sterile neutrinos?
- Can neutrinos generate matter-antimatter asymmetry of the universe?

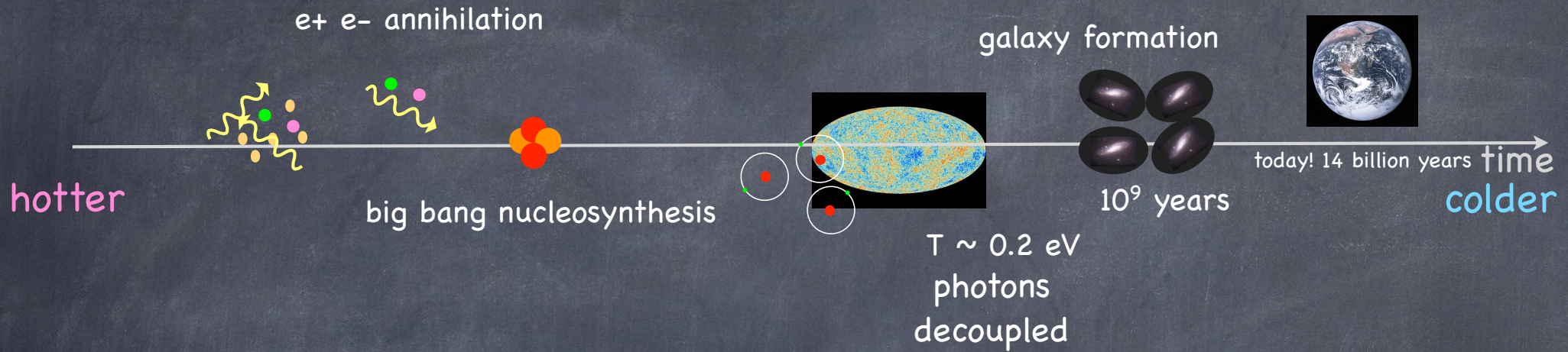
Astrophysics has previously informed neutrino physics!  
(solar neutrino problem  $\implies$  neutrino oscillations)



# Neutrinos in Cosmology

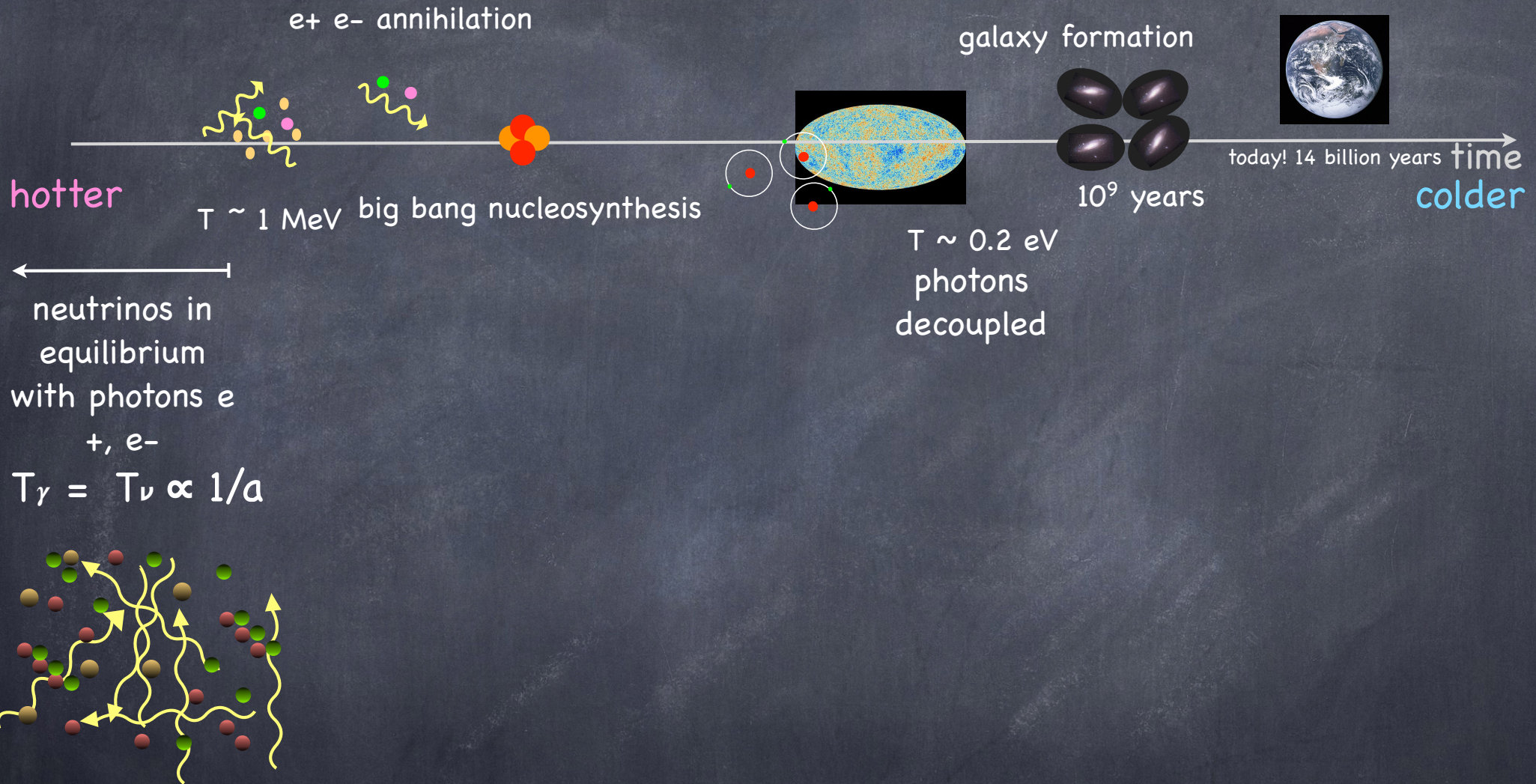


# Neutrinos in the Standard Cosmology



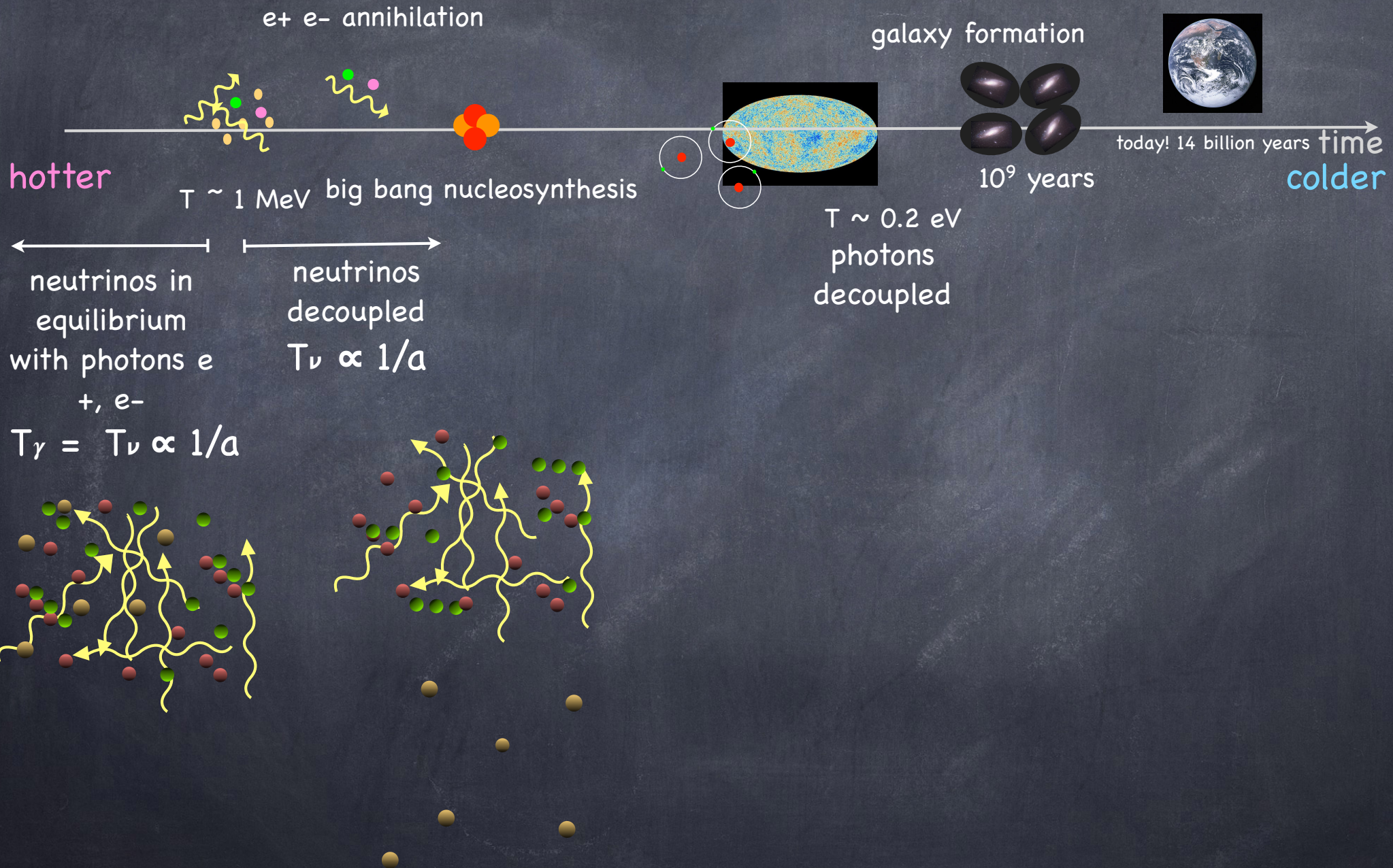


# Neutrinos in the Standard Cosmology



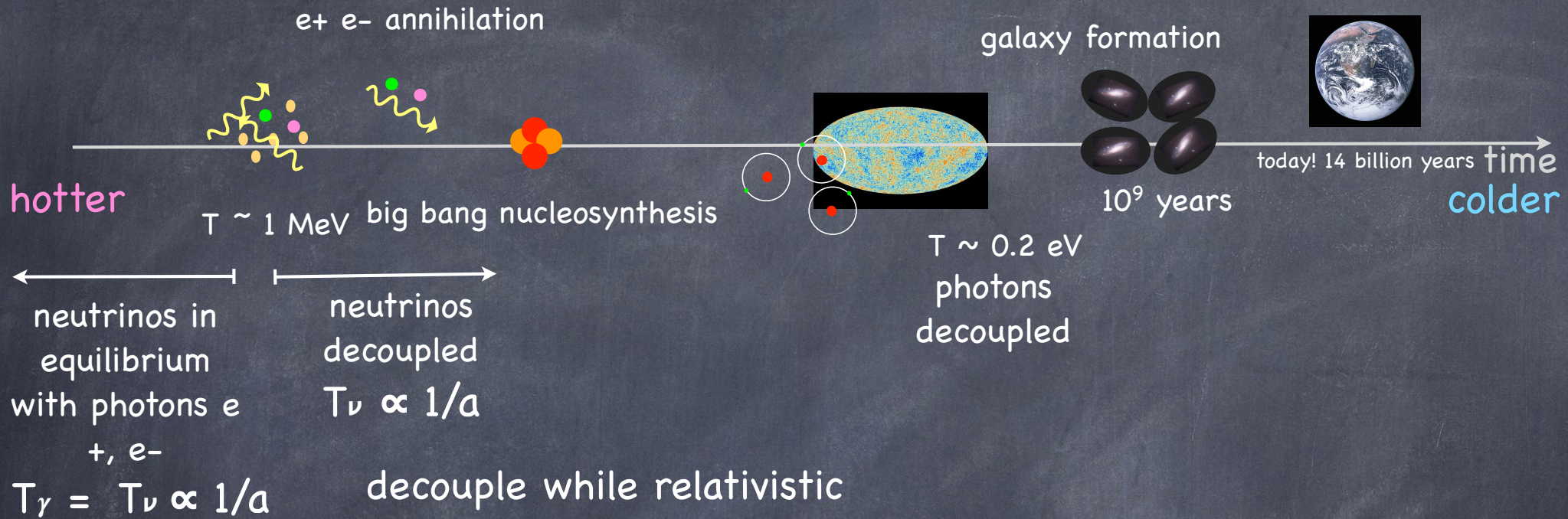


# Neutrinos in the Standard Cosmology





# Neutrinos in the Standard Cosmology

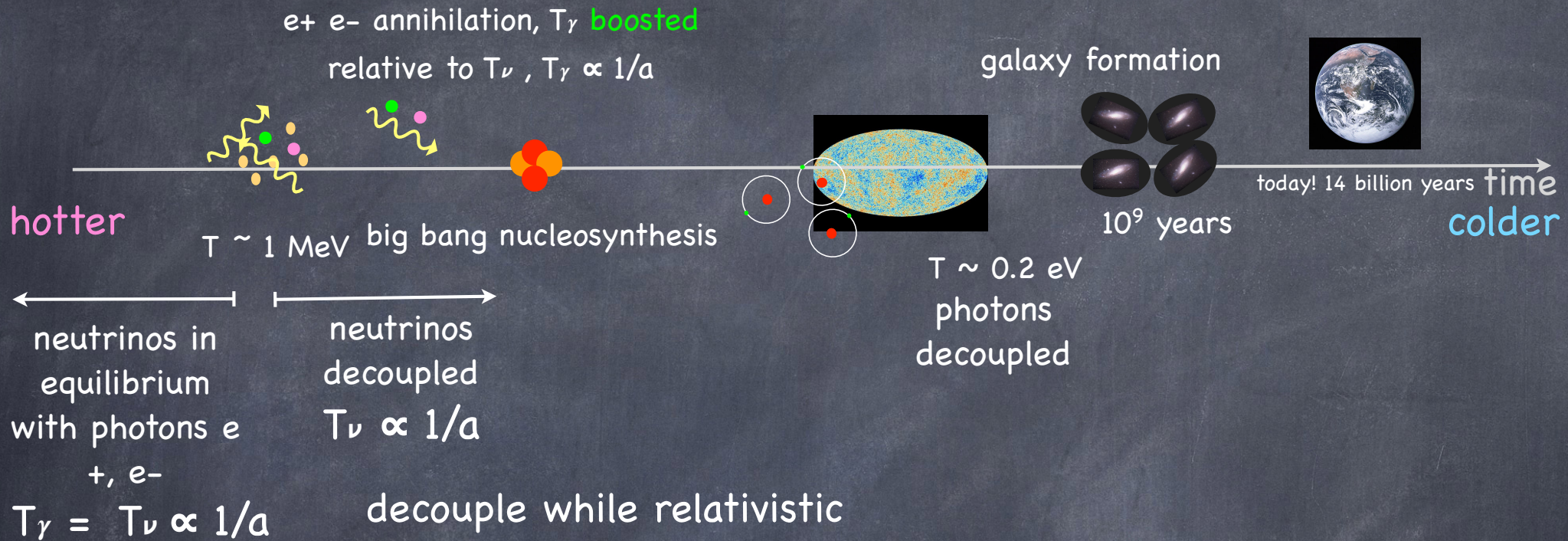


$$n_{1\nu} \sim T_\nu^3$$

$$\rho_{1\nu} \sim T_\nu^4$$



# Neutrinos in the Standard Cosmology



$$n_{1\nu} \sim T_\nu^3$$

$$\rho_{1\nu} \sim T_\nu^4$$

$$T_\gamma \approx \left(\frac{11}{4}\right)^{1/3} T_\nu$$

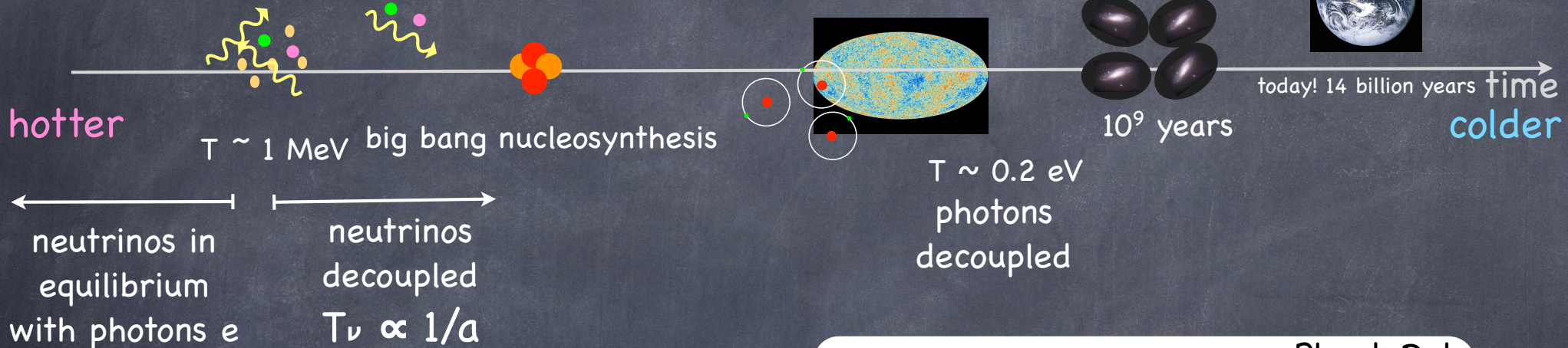
$$n_{1\nu} \approx 100/\text{cm}^3$$

$$T_\nu \approx 0.17 \text{ meV}$$



# Neutrinos in the Standard Cosmology

$e^+ e^-$  annihilation,  $T_\gamma$  **boosted**  
relative to  $T_\nu$ ,  $T_\gamma \propto 1/a$

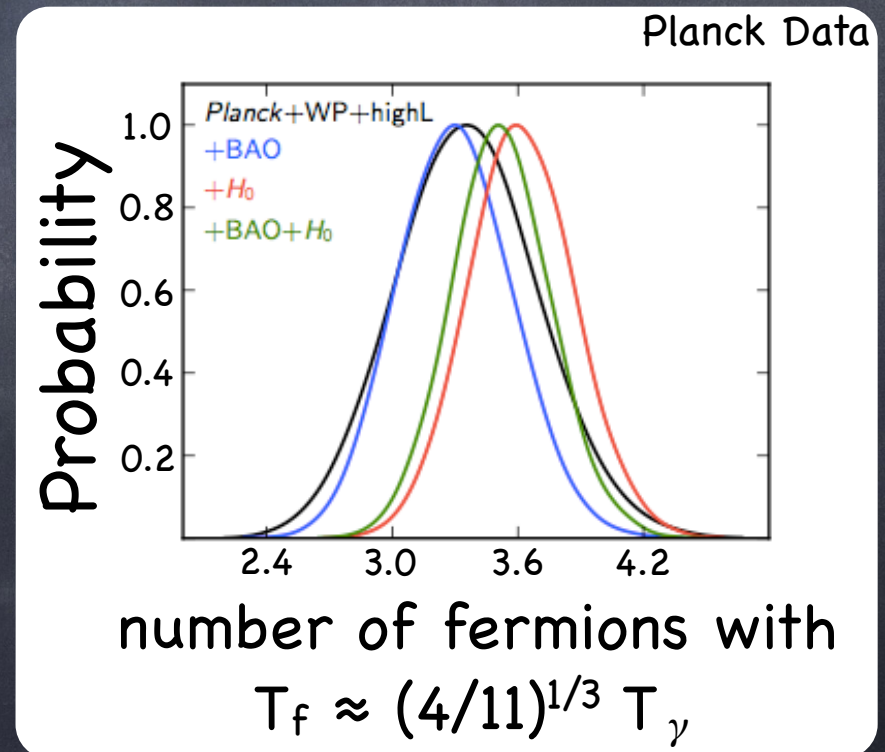


$$T_\gamma = T_\nu \propto 1/a$$

$$n_{1\nu} \sim T_\nu^3$$

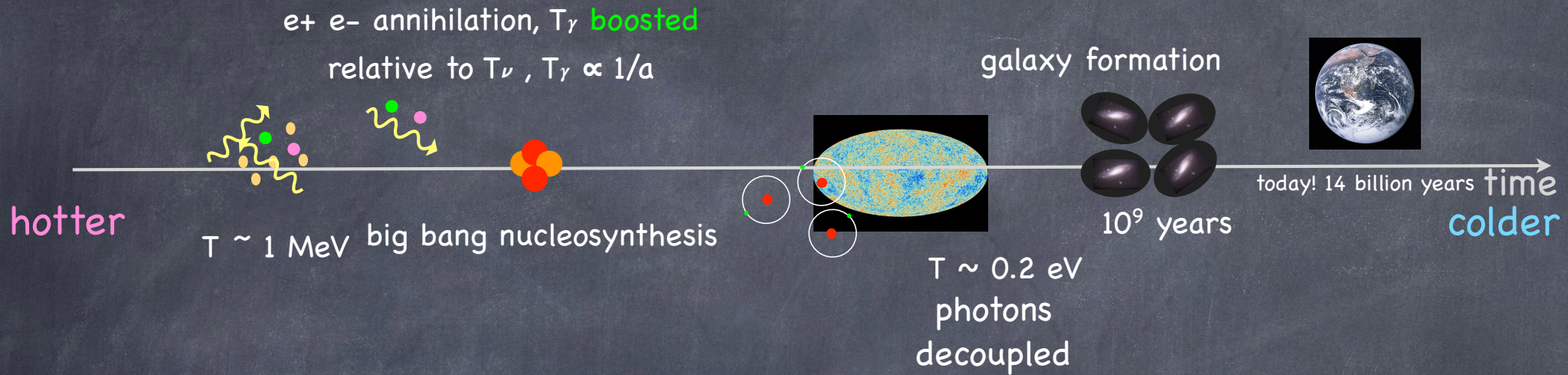
$$\rho_{1\nu} \sim T_\nu^4$$

$$T_\gamma \approx \left(\frac{11}{4}\right)^{1/3} T_\nu$$





# Neutrinos in the Standard Cosmology

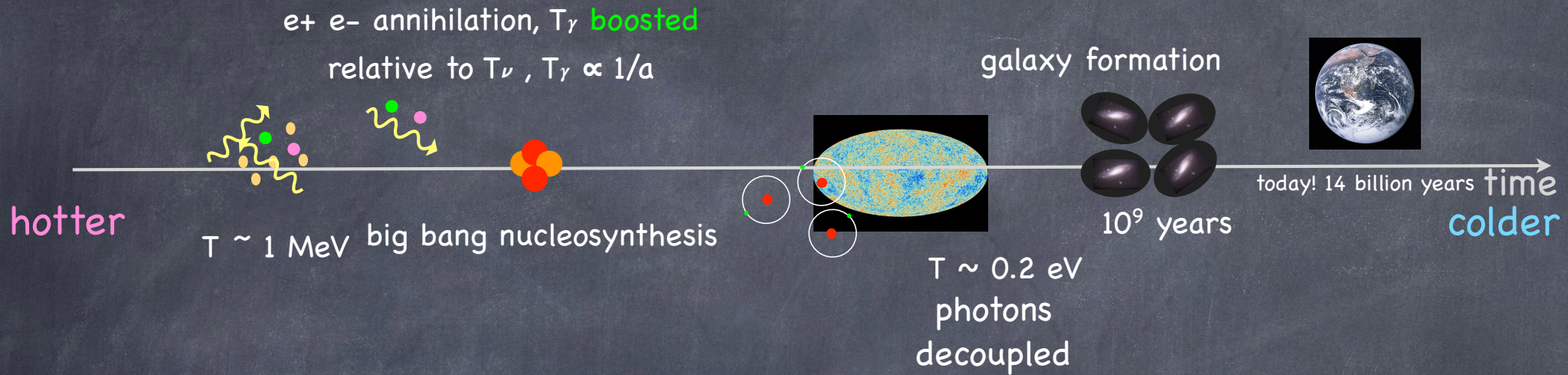


Once  $T_\nu \ll m_\nu$  energy density is just

$$\rho_\nu \approx \sum m_\nu n_\nu$$



# Neutrinos in the Standard Cosmology



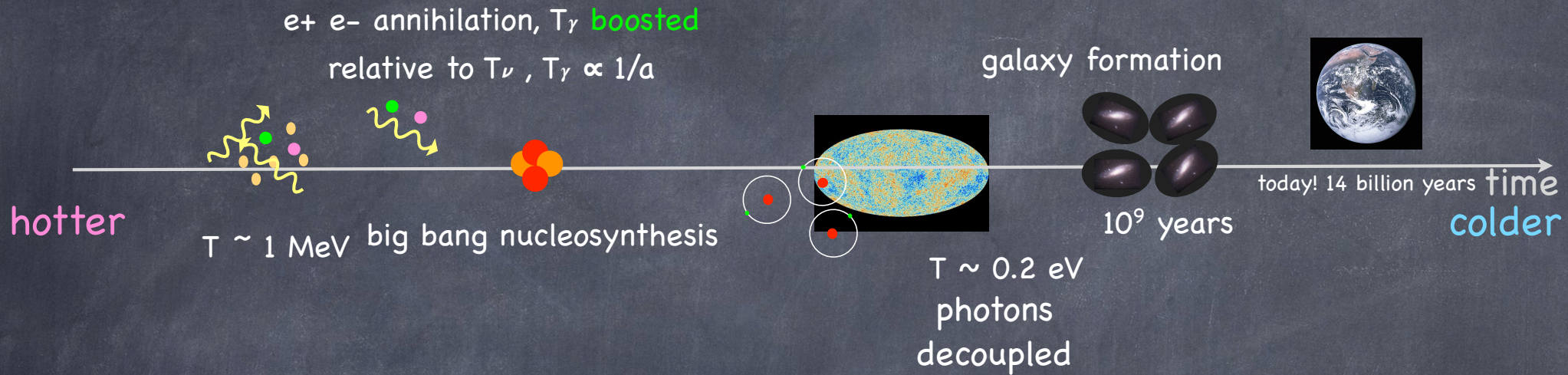
Once  $T_\nu \ll m_\nu$  energy density is just

$$\rho_\nu \approx \sum m_\nu n_\nu$$

$n_{1\nu}$  is known, so a measurement of  $\rho_\nu$  gives  $\sum m_\nu$



# Neutrinos in the Standard Cosmology



Once  $T_\nu \ll m_\nu$  energy density is just

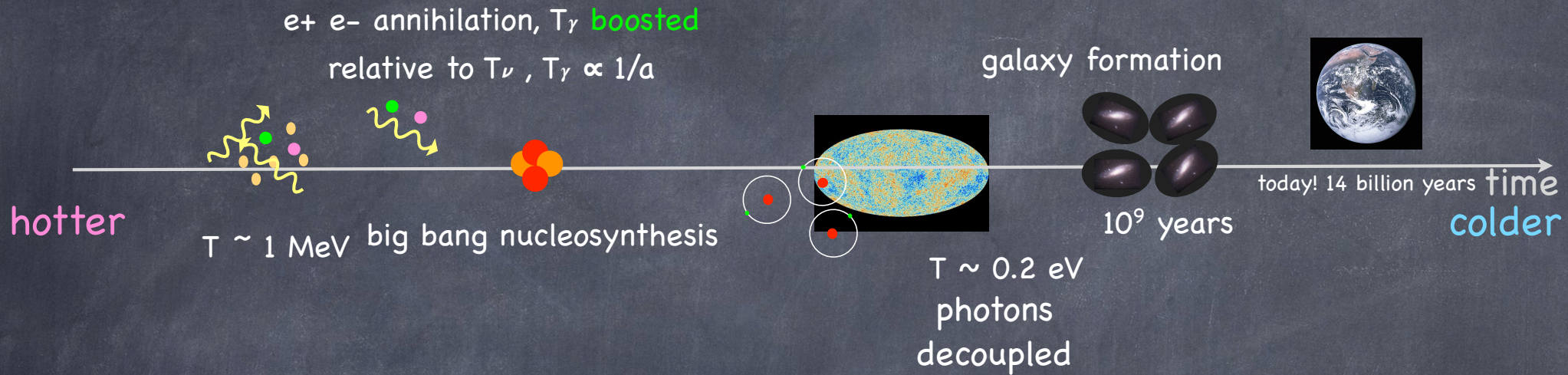
$$\rho_\nu \approx \sum m_\nu n_\nu$$

$n_{1\nu}$  is known, so a measurement of  $\rho_\nu$  gives  $\sum m_\nu$

Cosmology at later times, once  $T_\nu \ll m_\nu$ , tests  $\sum m_\nu$



# Neutrinos in the Standard Cosmology



Once  $T_\nu \ll m_\nu$  energy density is just

$$\rho_\nu \approx \sum m_\nu n_\nu$$

$n_{1\nu}$  is known, so a measurement of  $\rho_\nu$  gives  $\sum m_\nu$

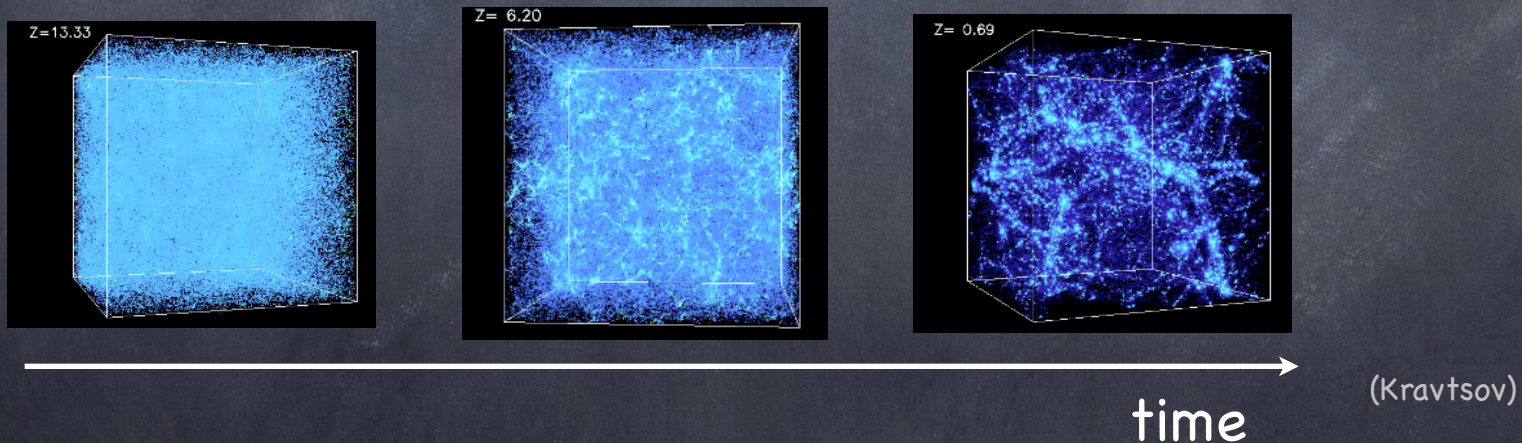
Cosmology at later times, once  $T_\nu \ll m_\nu$ , tests  $\sum m_\nu$



Large-scale Structure



# Neutrinos in Large-scale structure





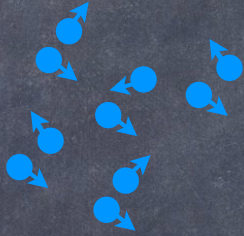
# Massive neutrinos and linear structure growth

The gravitational evolution of large-scale structure is different for **fast** and **slow** moving particles



# Massive neutrinos and linear structure growth

The gravitational evolution of large-scale structure is different for **fast** and **slow** moving particles



(clump easily)

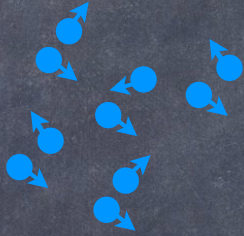


(don't clump easily)



# Massive neutrinos and linear structure growth

The gravitational evolution of large-scale structure is different for **fast** and **slow** moving particles



(clump easily)

baryons and cold dark  
matter

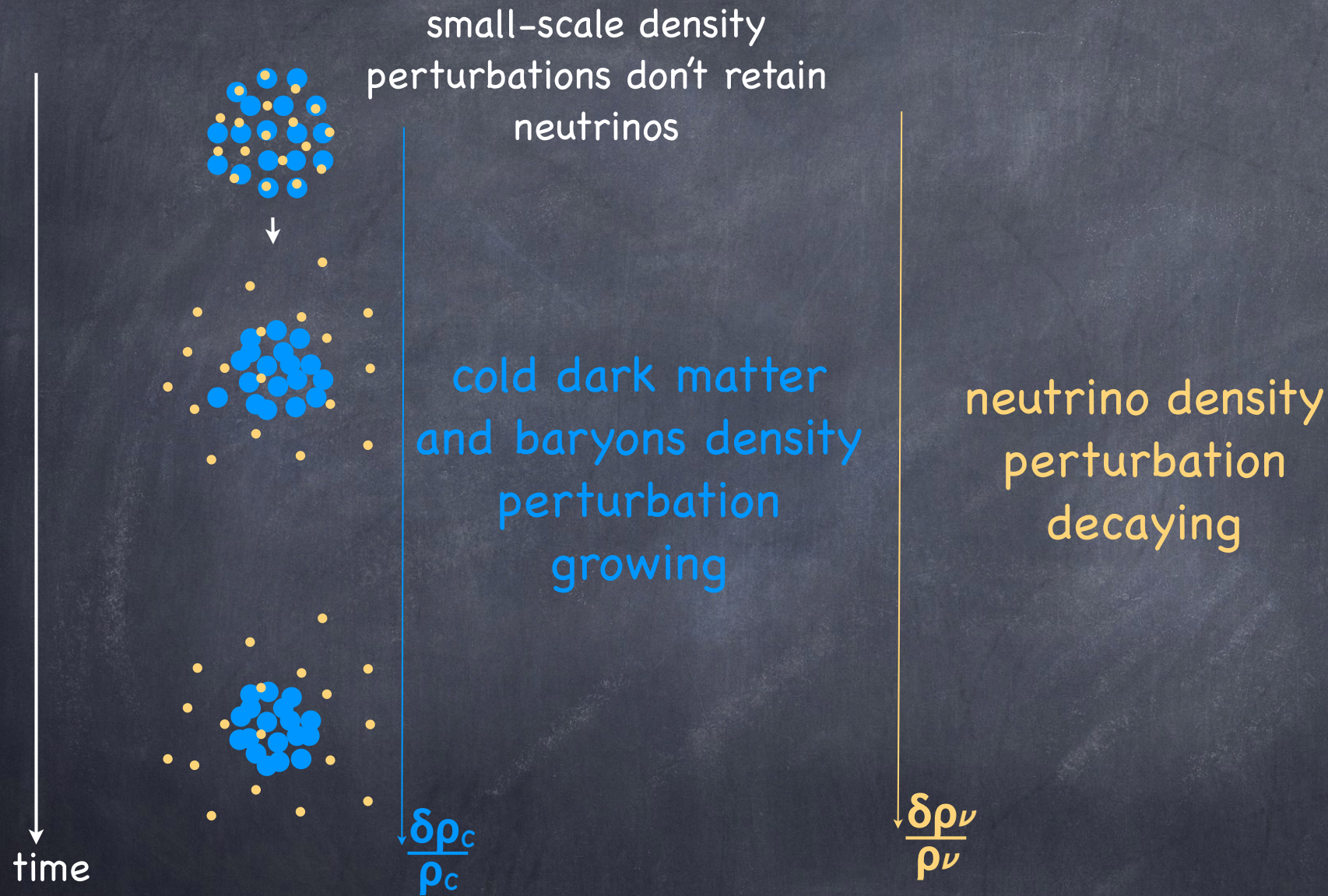


(don't clump easily)

neutrinos (or other  
exotic light dark  
matter)

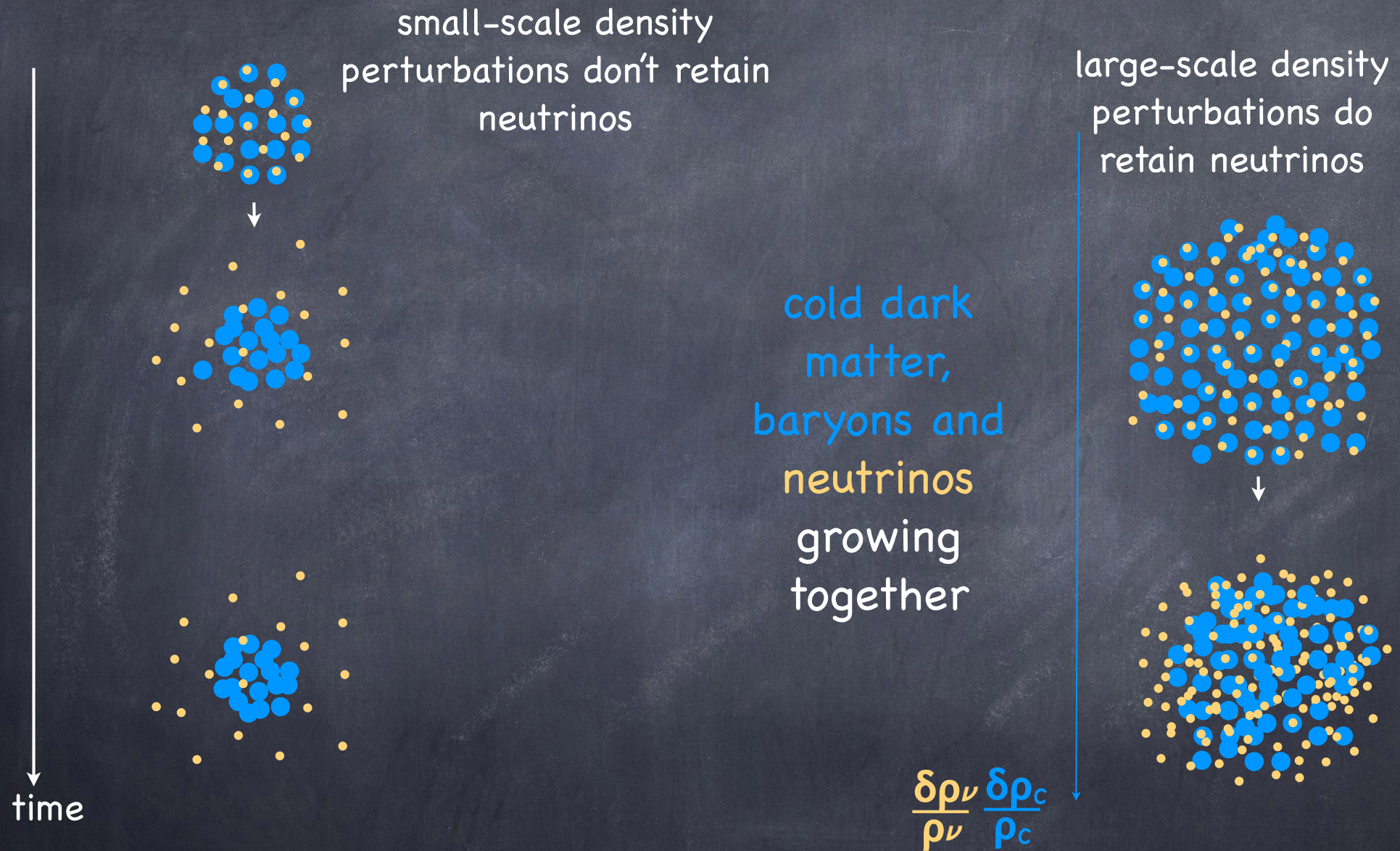


# Massive neutrinos and linear structure growth



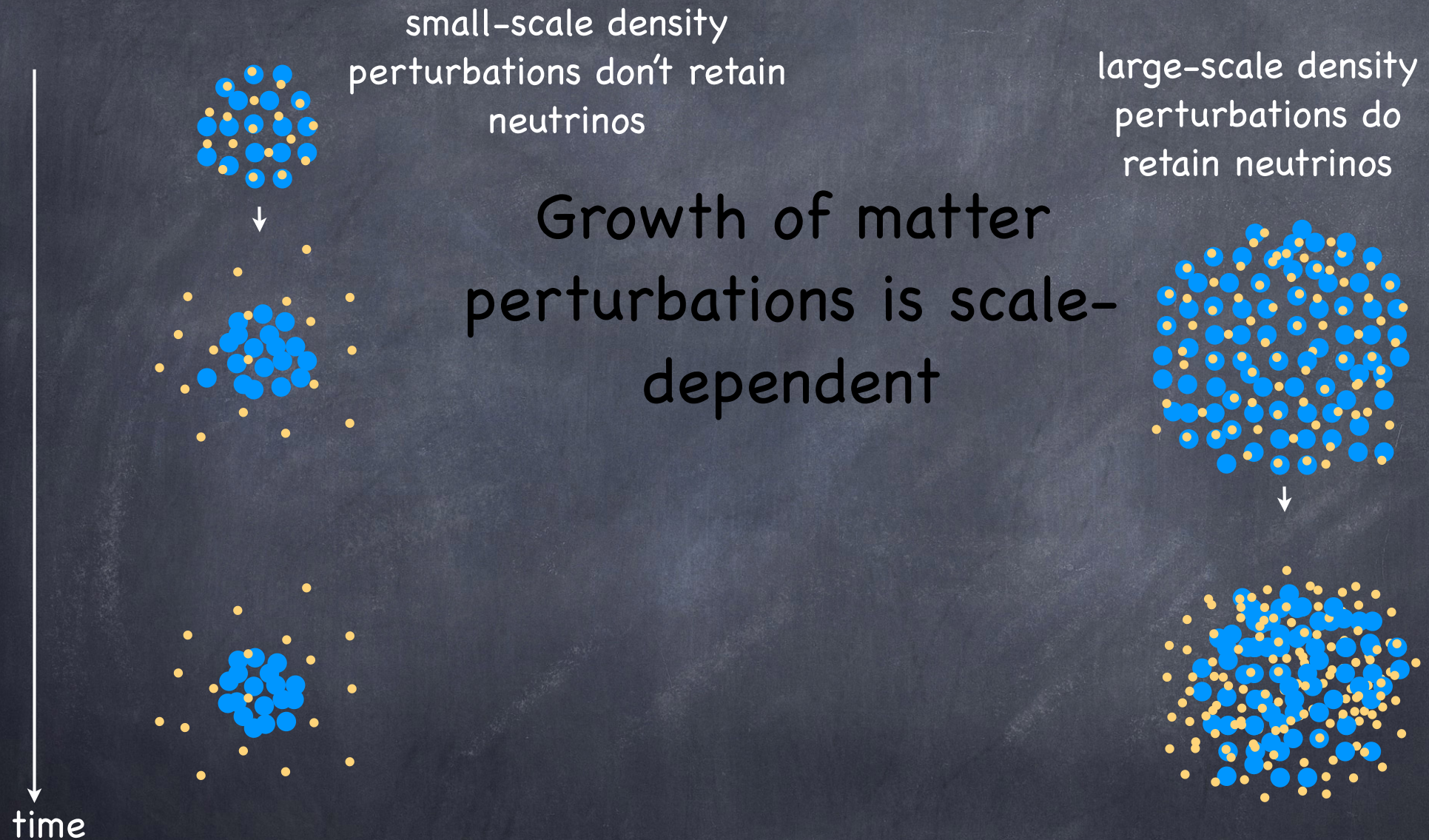


# Massive neutrinos and linear structure growth



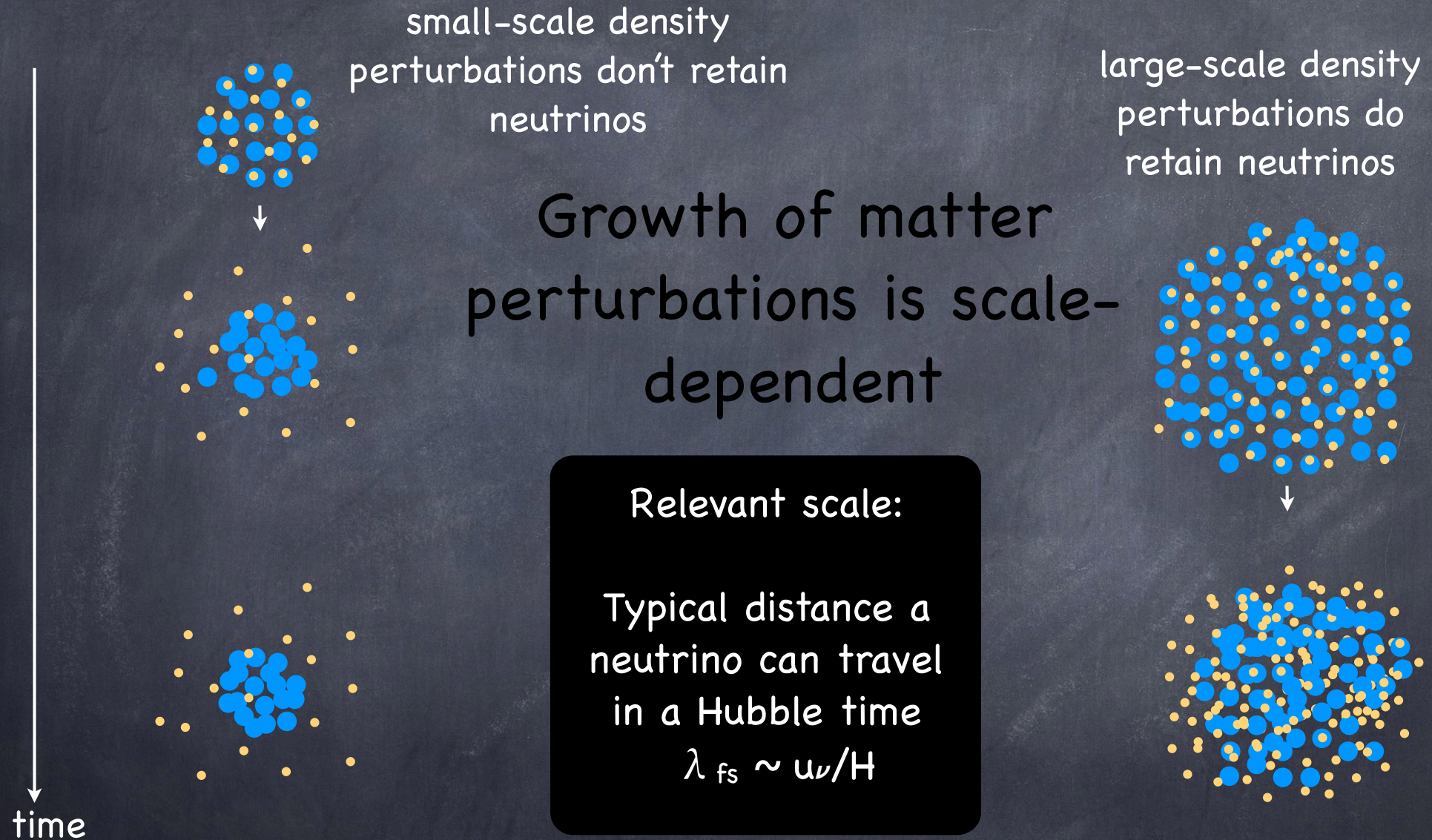


# Massive neutrinos and linear structure growth



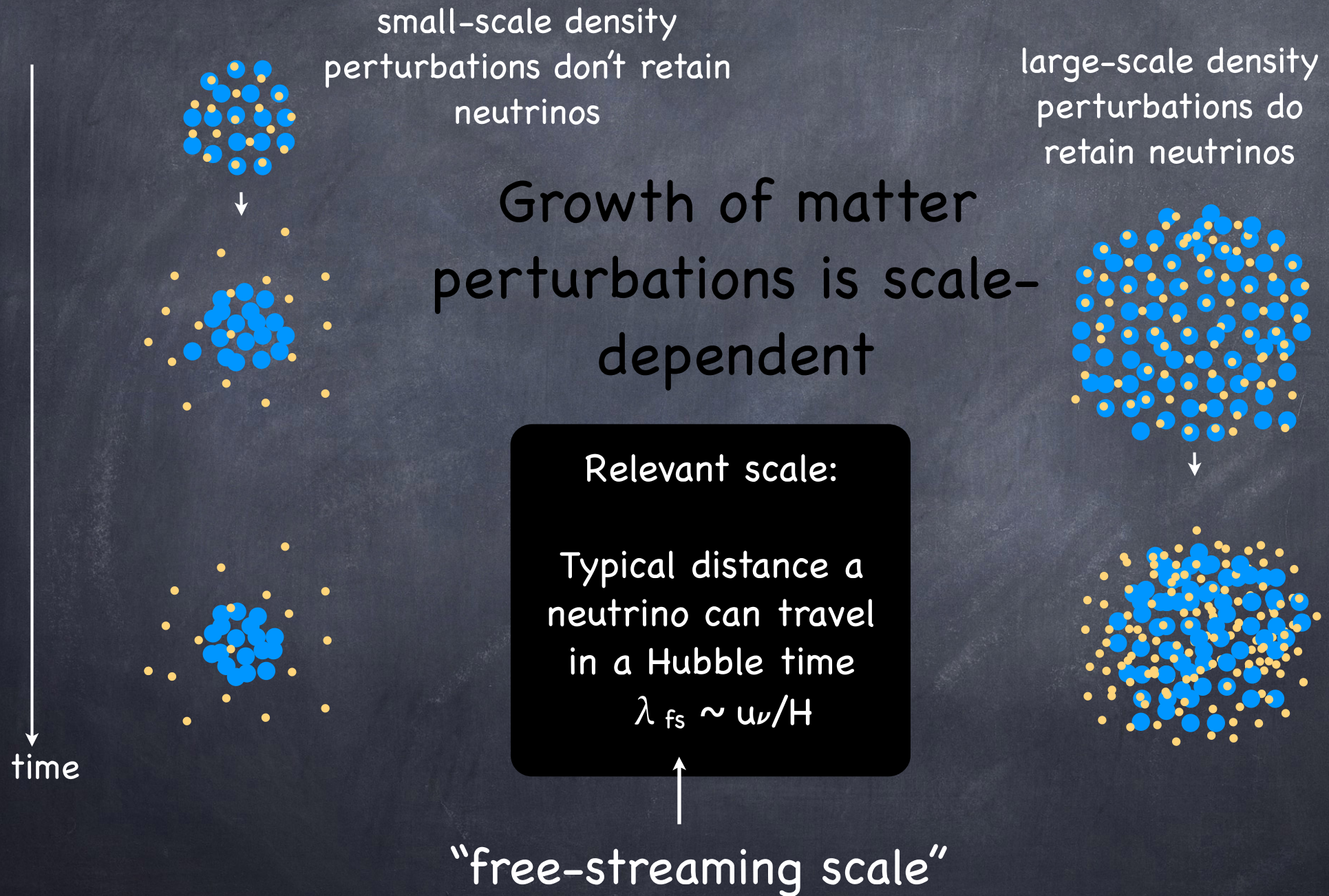


# Massive neutrinos and linear structure growth



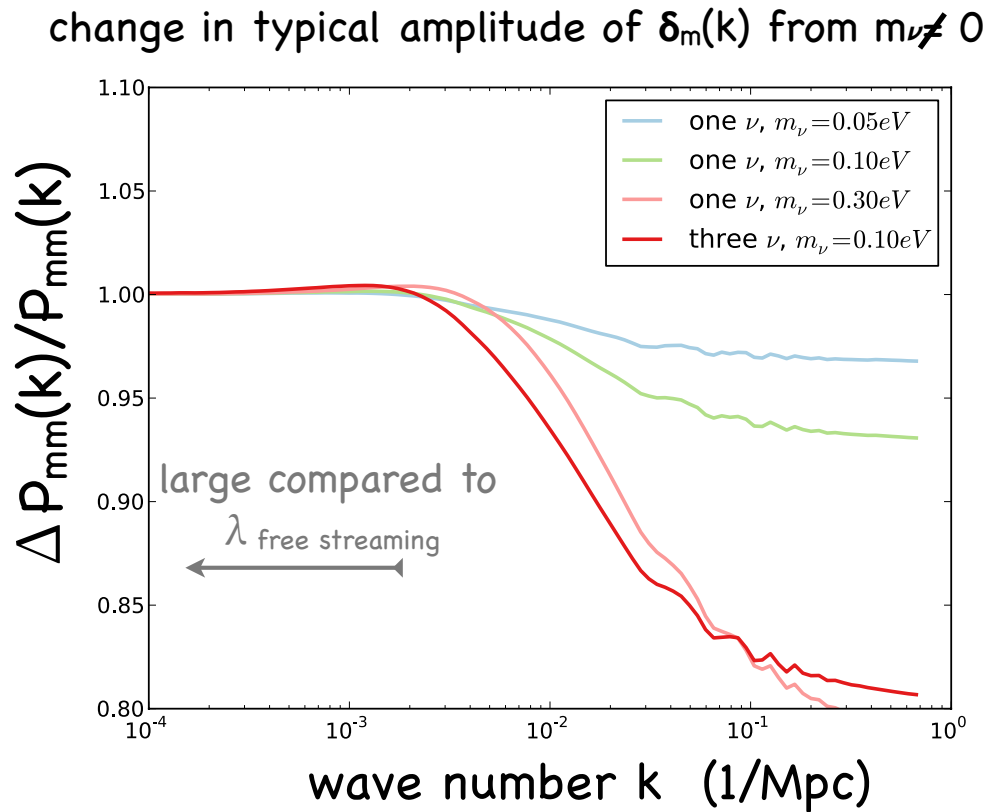


# Massive neutrinos and linear structure growth





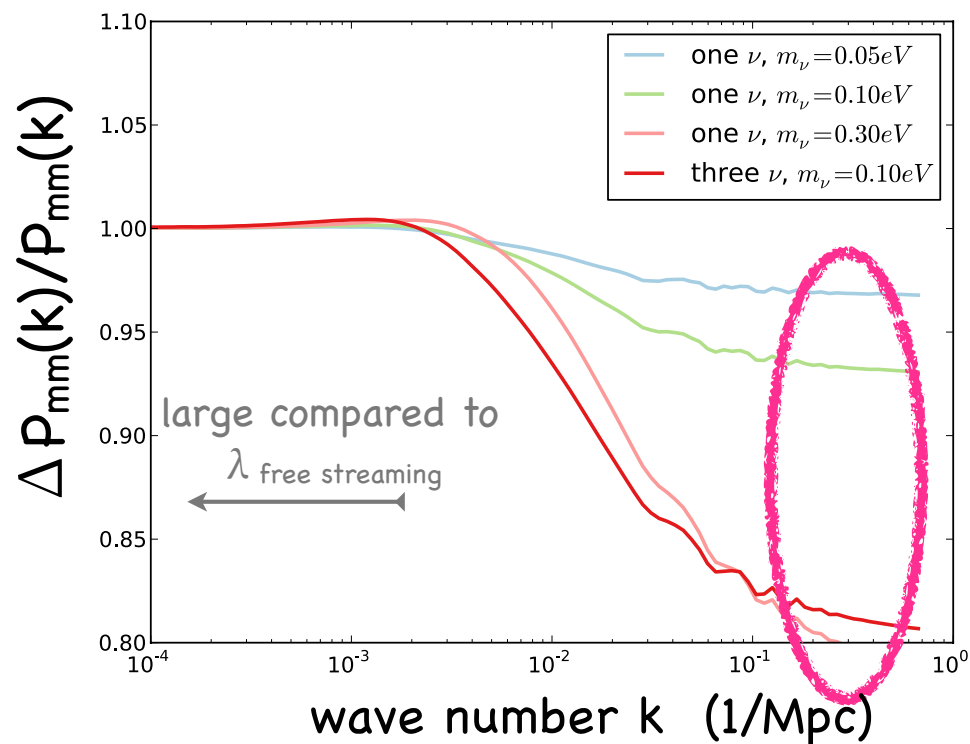
# Scale-dependent growth



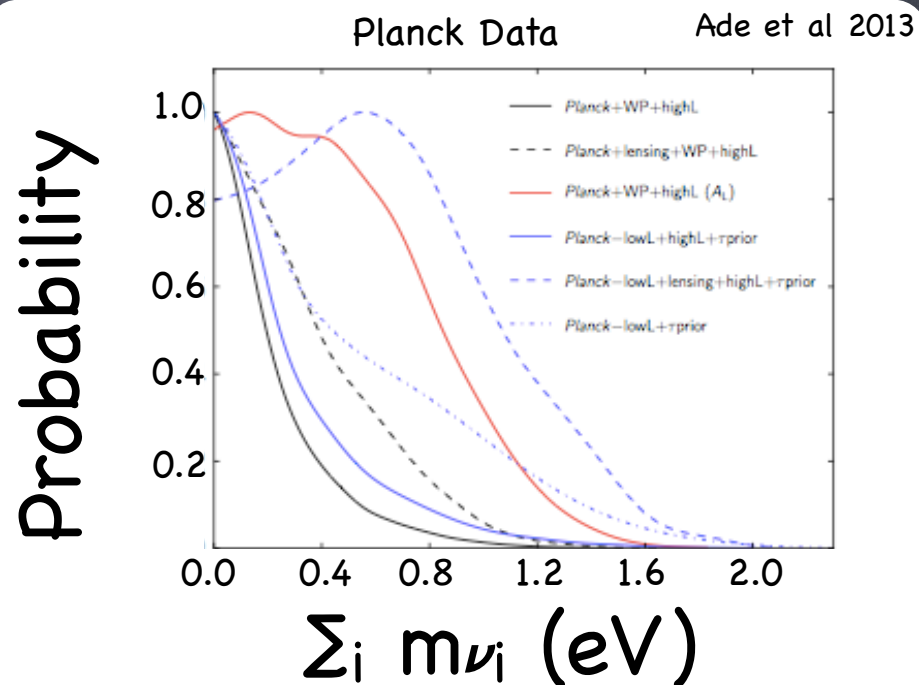


# Scale-dependent growth

change in typical amplitude of  $\delta_m(k)$  from  $m_\nu \neq 0$



cosmological constraints!





So, massive neutrinos change the amplitude and growth rate of matter perturbations below the neutrino free-streaming scale



So, massive neutrinos change the amplitude and growth rate of matter perturbations below the neutrino free-streaming scale

Some observable consequences:



So, massive neutrinos change the amplitude and growth rate of matter perturbations below the neutrino free-streaming scale

Some observable consequences:

- Suppressed matter power spectrum (test via lensing, galaxy power spectra)



So, massive neutrinos change the amplitude and growth rate of matter perturbations below the neutrino free-streaming scale

Some observable consequences:

- Suppressed matter power spectrum (test via lensing, galaxy power spectra)
- Fewer massive halos hosting galaxy clusters



So, massive neutrinos change the amplitude and growth rate of matter perturbations below the neutrino free-streaming scale

Some observable consequences:

- Suppressed matter power spectrum (test via lensing, galaxy power spectra)
- Fewer massive halos hosting galaxy clusters
  - (But neutrino halos eventually accumulate around the cold dark matter halos!)



So, massive neutrinos change the amplitude and growth rate of matter perturbations below the neutrino free-streaming scale

Some observable consequences:

- Suppressed matter power spectrum (test via lensing, galaxy power spectra)
- Fewer massive halos hosting galaxy clusters
  - (But neutrino halos eventually accumulate around the cold dark matter halos!)
- Scale-dependent halo bias



So, massive neutrinos change the amplitude and growth rate of matter perturbations below the neutrino free-streaming scale

Some observable consequences:

- Suppressed matter power spectrum (test via lensing, galaxy power spectra)
- Fewer massive halos hosting galaxy clusters (ML 2014)
  - (But neutrino halos eventually accumulate around the cold dark matter halos!) (ML & Zaldarriaga 2013)
- Scale-dependent halo bias (ML 2014)



So, massive neutrinos change the amplitude and growth rate of matter perturbations below the neutrino free-streaming scale

Some observable consequences:

- Suppressed matter power spectrum (test via lensing, galaxy power spectra)
- Fewer massive halos hosting galaxy clusters (ML 2014)
  - (But neutrino halos eventually accumulate around the cold dark matter halos!)

(ML & Zaldarriaga 2013)

 Scale-dependent halo bias

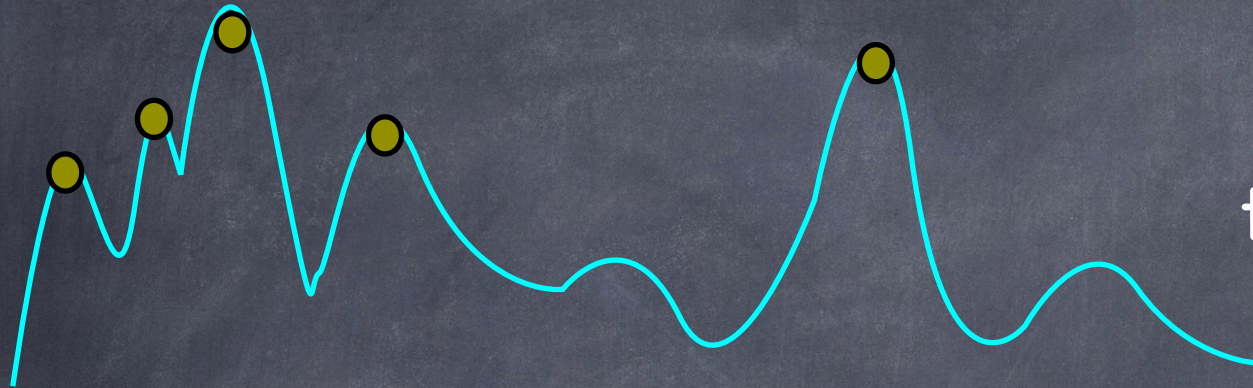
(ML 2014)



Scale-dependent halo  
bias from massive  
neutrinos



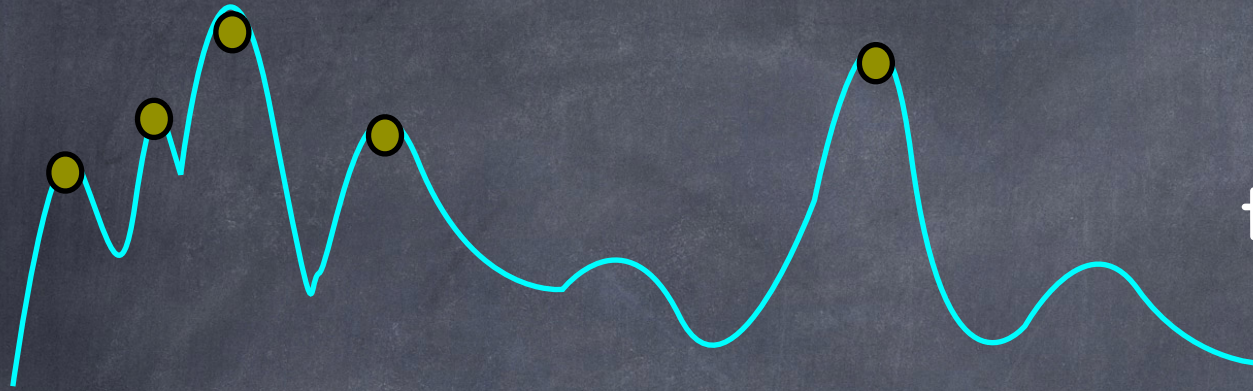
# Scale-dependent bias — main idea:



**halos** are biased  
tracers of the **matter**  
**density field**

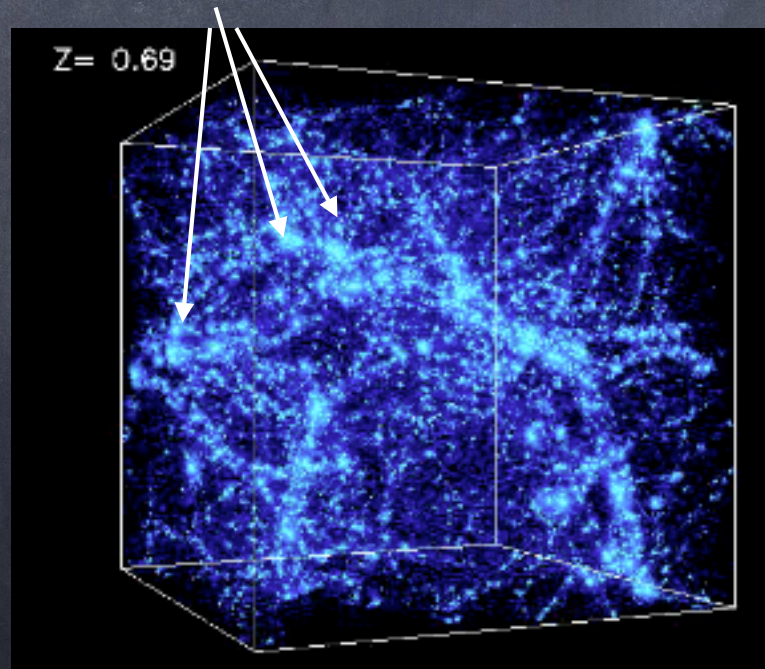


# Scale-dependent bias — main idea:



**halos** are biased  
tracers of the **matter**  
**density field**

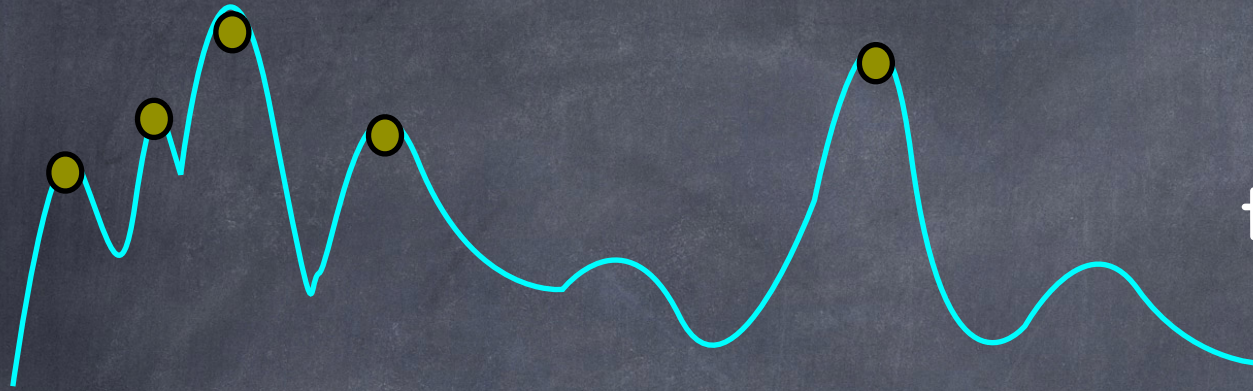
(these nodes are **cold dark matter halos**)



(Kravtsov)

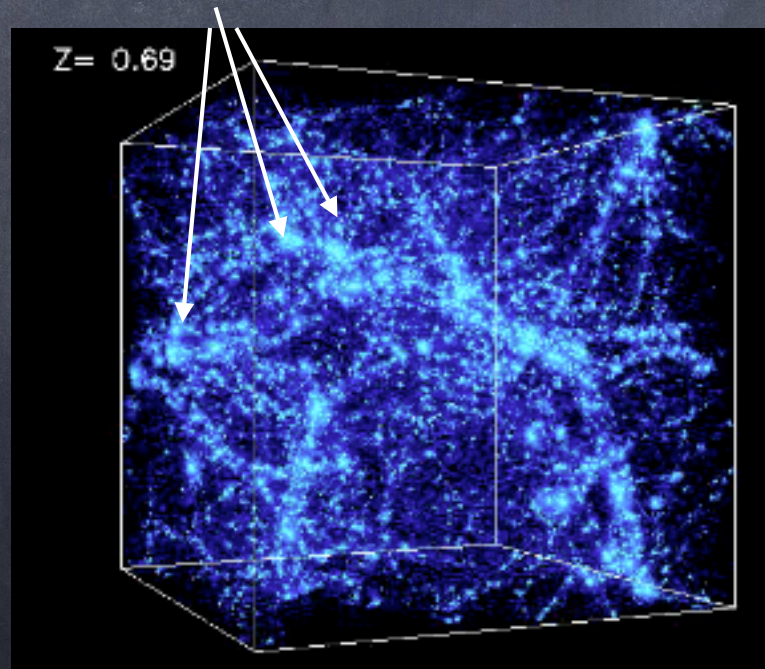


# Scale-dependent bias — main idea:



**halos** are biased tracers of the **matter density field**

(these nodes are **cold dark matter halos**)

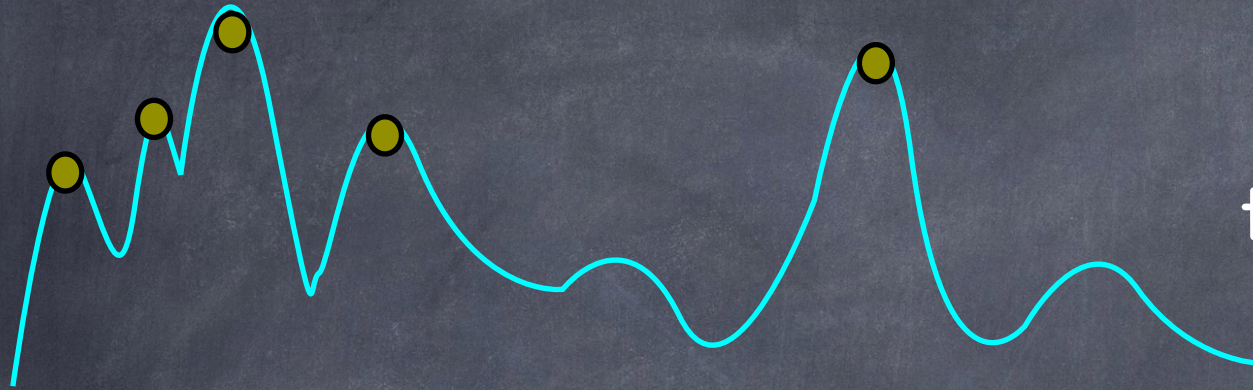


i.e. gravitationally bound blobs of dark matter where galaxies and clusters of galaxies live

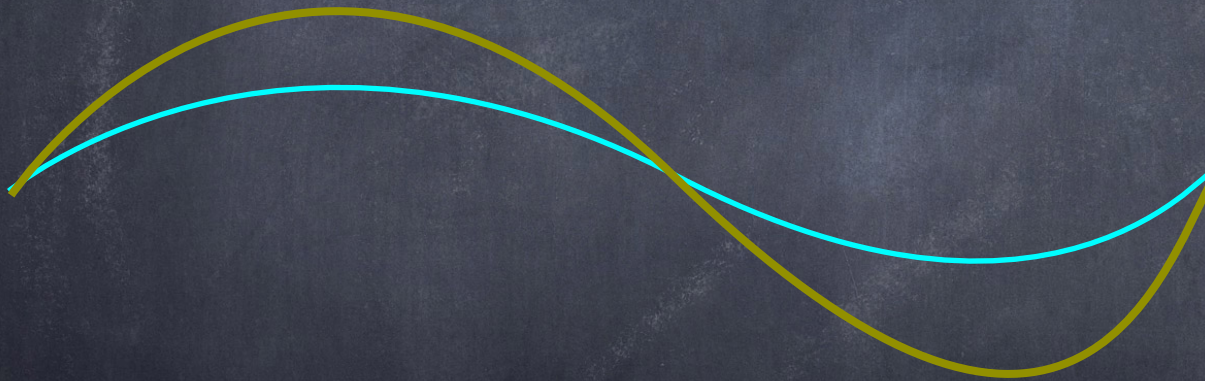
(Kravtsov)



# Scale-dependent bias — main idea:



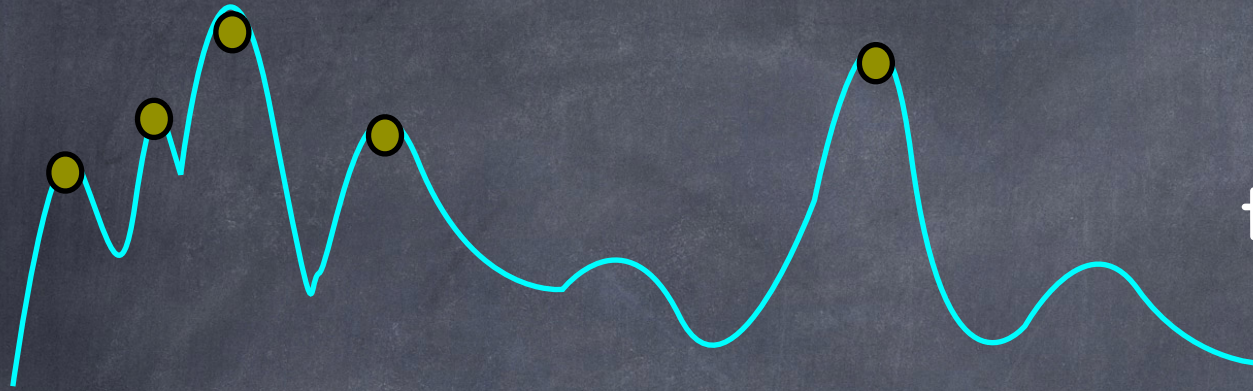
**halos** are biased tracers of the **matter density** field



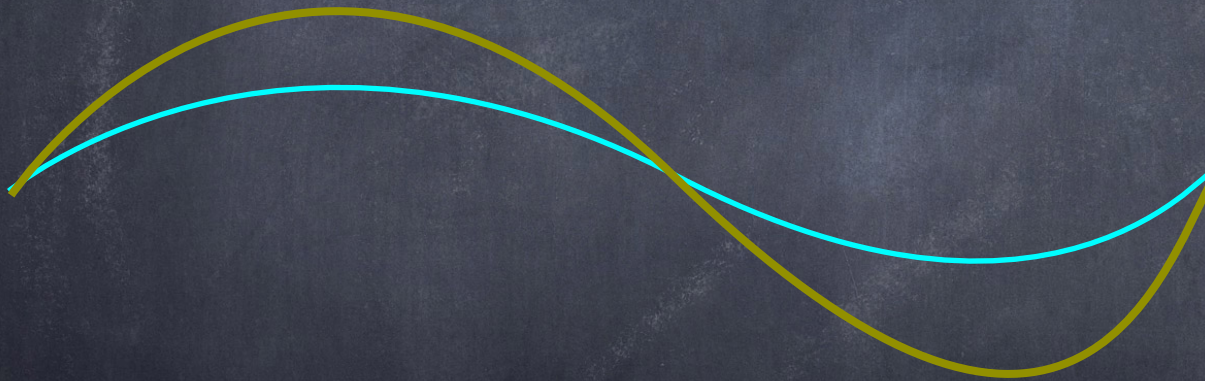
the **number density of halos** is modulated by long-wavelength fluctuations in the **matter density** field



# Scale-dependent bias — main idea:



**halos** are biased tracers of the **matter density** field



the **number density** of **halos** is modulated by long-wavelength fluctuations in the **matter density** field

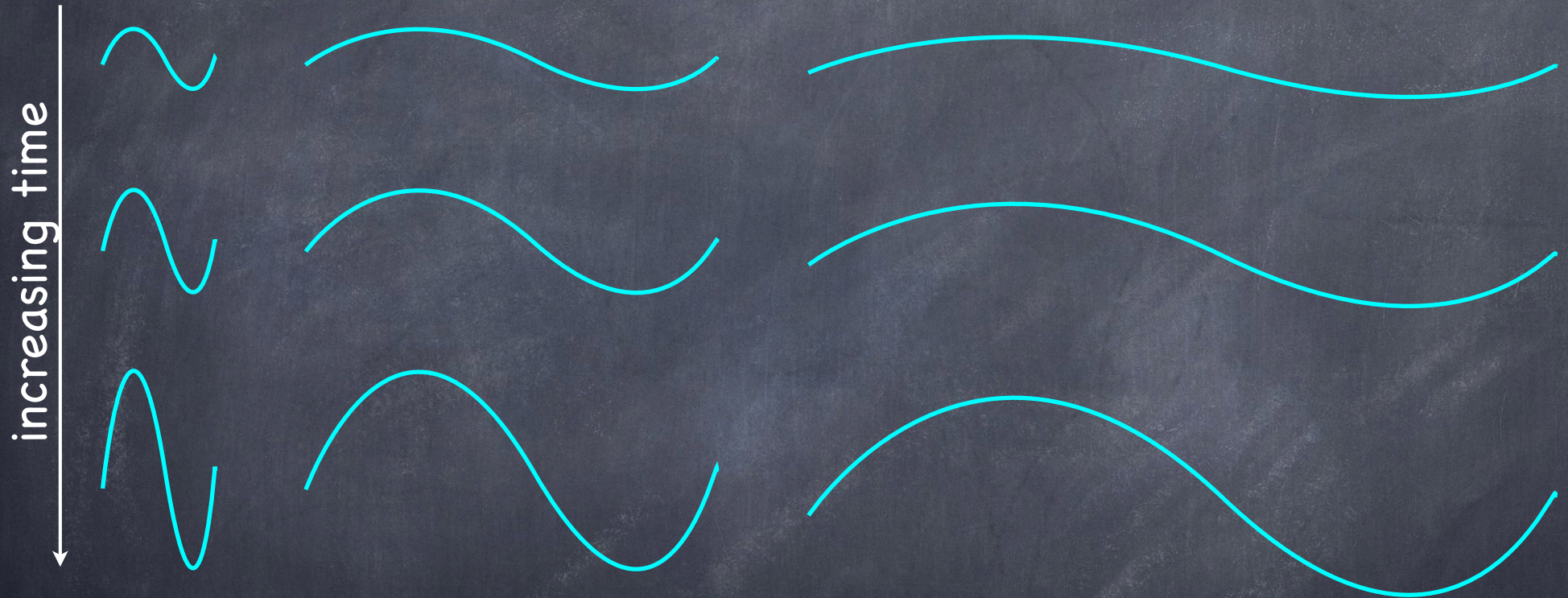
$$\frac{\delta n}{n} \equiv b \left. \frac{\delta \rho}{\rho} \right|_{\text{long-wavelength}}$$

**b** is the halo bias



# Scale-dependent bias — main idea:

In a universe with CDM only, the linear evolution of **matter fluctuations** is independent of their wavelength

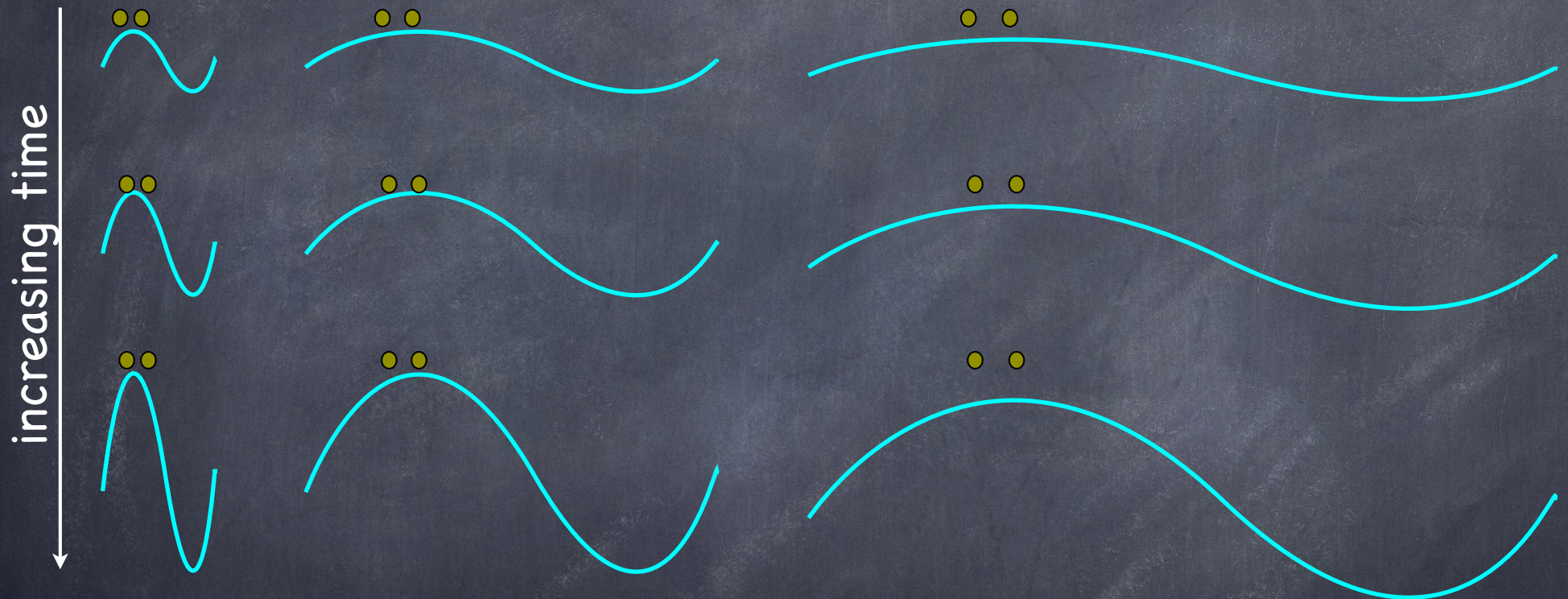


$$\frac{\delta\rho}{\rho}(k, z_{\text{final}}) \propto D(z_{\text{final}}) \frac{\delta\rho}{\rho}(k, z_{\text{initial}})$$



# Scale-dependent bias — main idea:

In a universe with CDM only, the linear evolution of **matter fluctuations** is independent of their wavelength



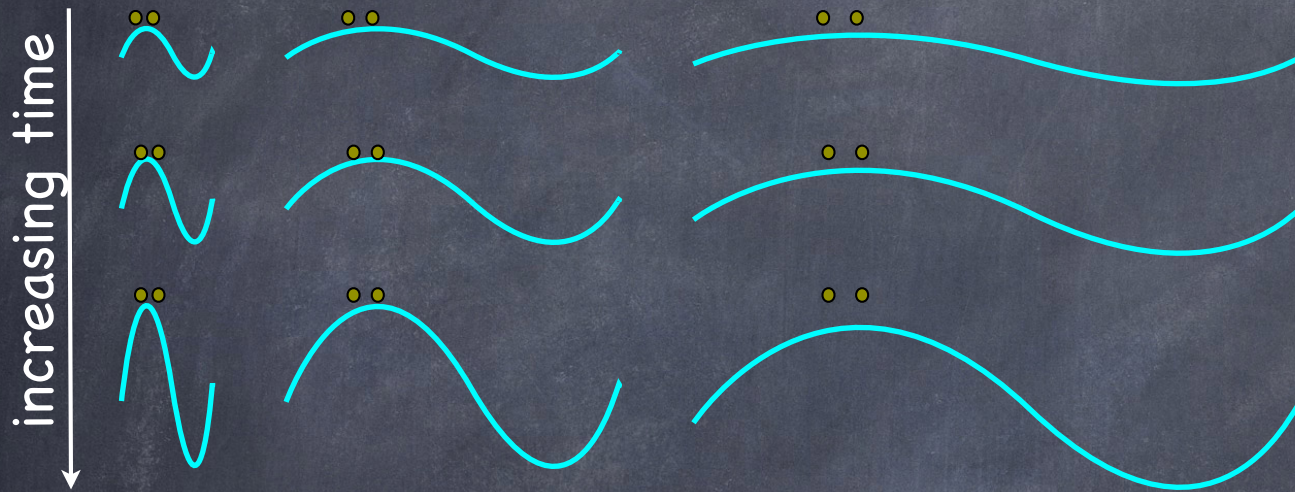
$$\frac{\delta\rho}{\rho}(k, z_{\text{final}}) \propto D(z_{\text{final}}) \frac{\delta\rho}{\rho}(k, z_{\text{initial}})$$

**halos** can't tell the wavelength of the background **matter** density perturbation



# Scale-dependent bias — main idea:

In a universe with CDM only, the linear evolution of **matter fluctuations** is independent of their wavelength



**halos** can't tell the wavelength of the background **matter** density perturbation

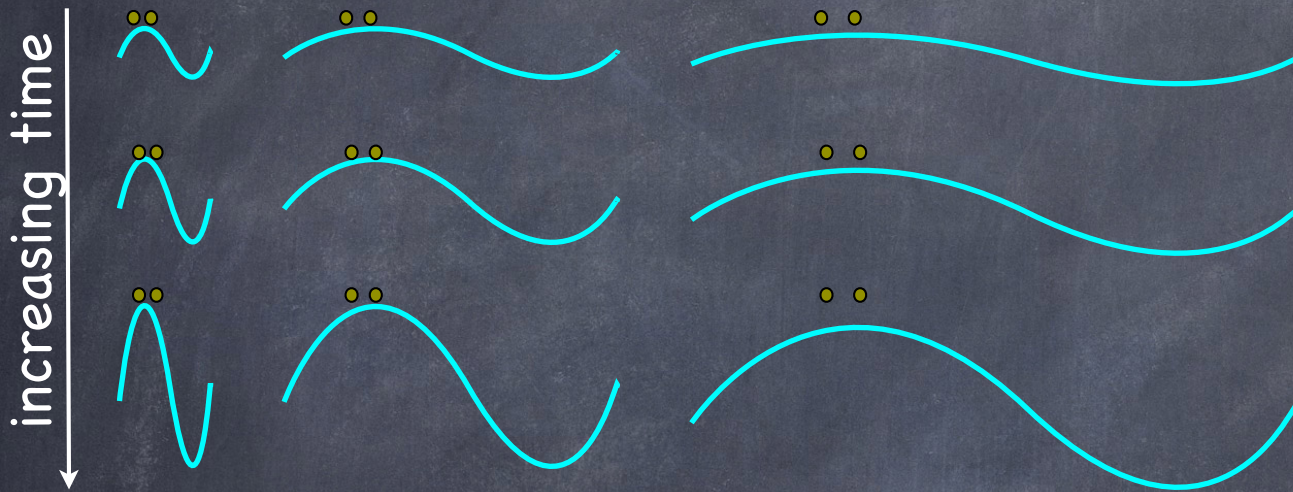


the effect of  $\frac{\delta\rho}{\rho}$  on the **halo field** (the linear bias) is independent of  $k$



# Scale-dependent bias — main idea:

In a universe with CDM only, the linear evolution of **matter fluctuations** is independent of their wavelength



**halos** can't tell the wavelength of the background **matter** density perturbation



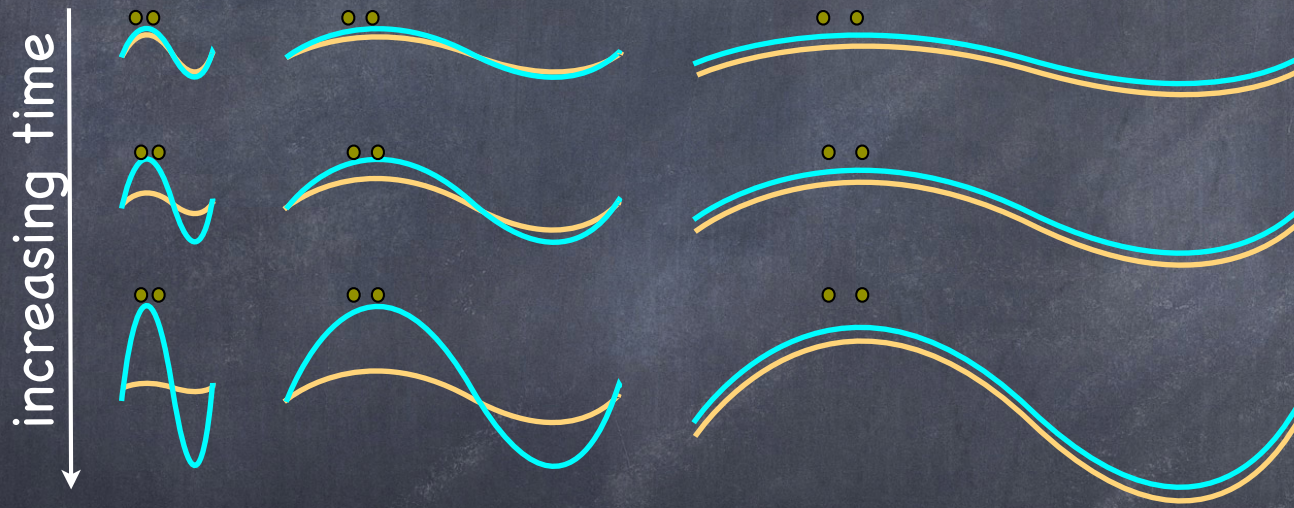
the effect of  $\frac{\delta\rho}{\rho}$  on the **halo field** (the linear bias) is independent of  $k$

**massive neutrinos break this**

**halo bias can depend on  $k$**



# Scale-dependent bias — main idea:

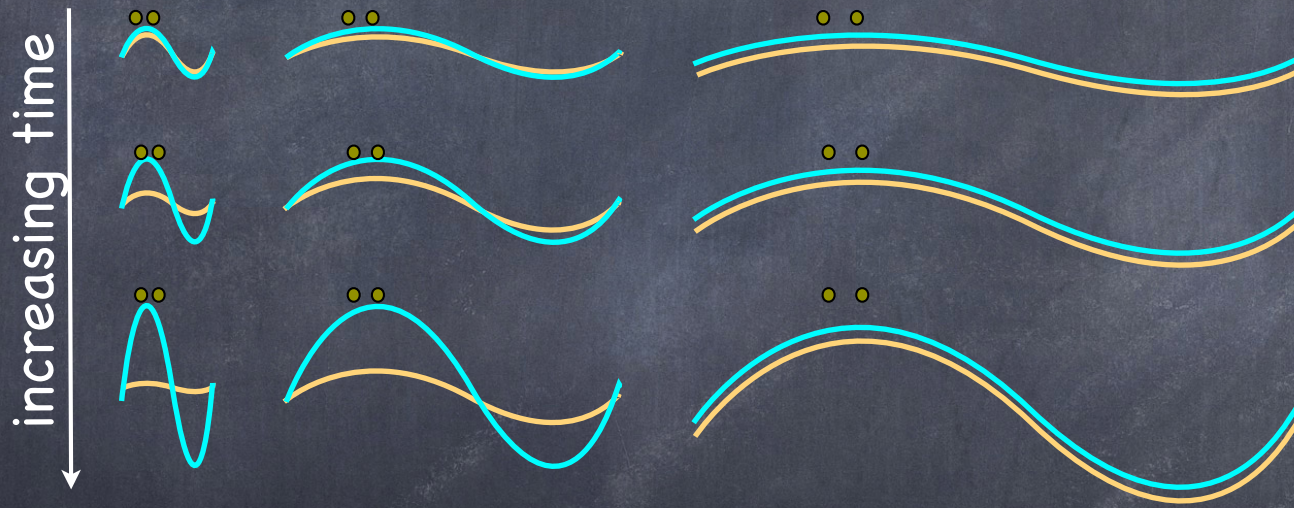


halos  
neutrinos  
cold dark matter



# Scale-dependent bias — main idea:

WANT: estimate of  $k$ -dependence of  
the halo bias caused by **massive**  
**neutrinos**

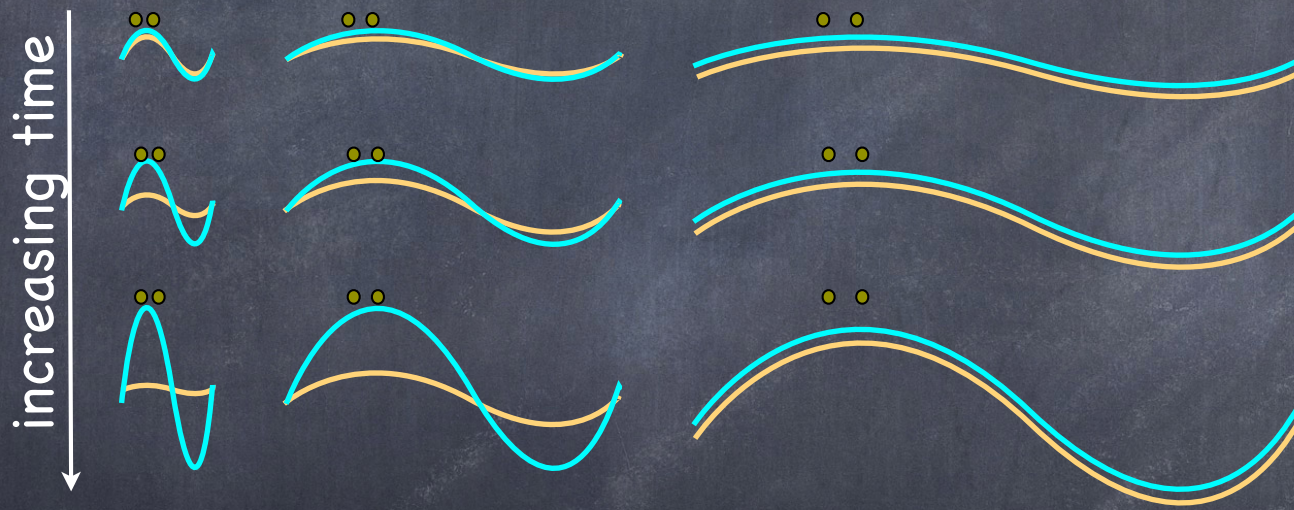


halos  
neutrinos  
cold dark matter



# Scale-dependent bias — main idea:

WANT: estimate of  $k$ -dependence of  
the halo bias caused by **massive  
neutrinos**



halos  
neutrinos  
cold dark matter

( see also Hui & Parfrey 2008; Parfrey, Hui, Sheth 2011;)



# Scale-dependent bias

The scale-dependent growth of density perturbations causes halo bias to be scale dependent



# Scale-dependent bias

The scale-dependent growth of density perturbations causes halo bias to be scale dependent

$$\frac{\delta n}{n}(k) = b \frac{\delta \rho_m}{\rho_m}(k) \quad \longrightarrow \quad \frac{\delta n}{n}(k) = b(k) \frac{\delta \rho_m}{\rho_m}(k)$$



Scale-dependent bias

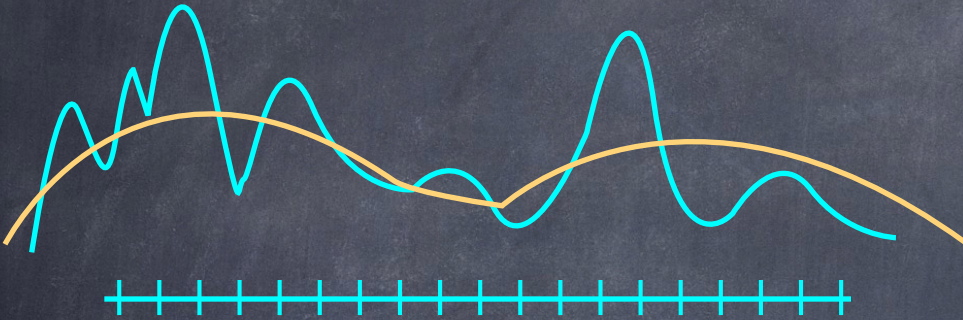
Prescription for  
calculating the halo  
bias in a universe with  
massive neutrinos



# Scale-dependent bias

## Prescription for calculating the halo bias

initial density field



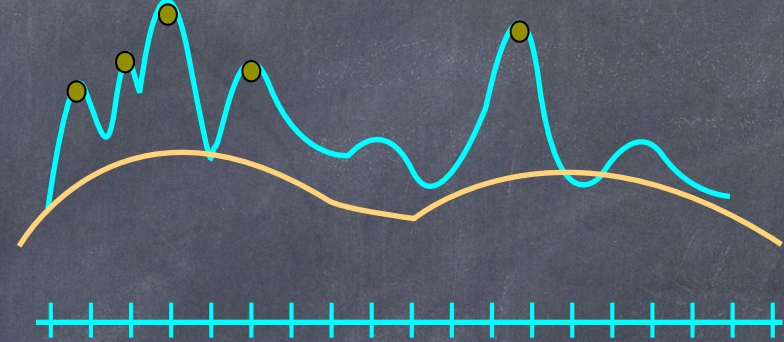
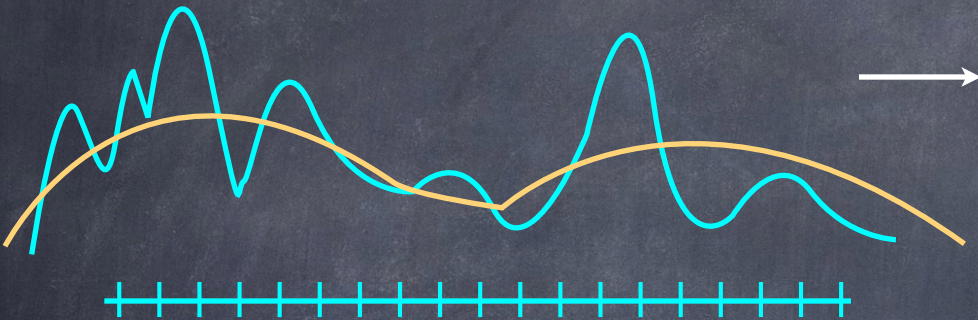


# Scale-dependent bias

## Prescription for calculating the halo bias

initial density field

initial proto-halo distribution

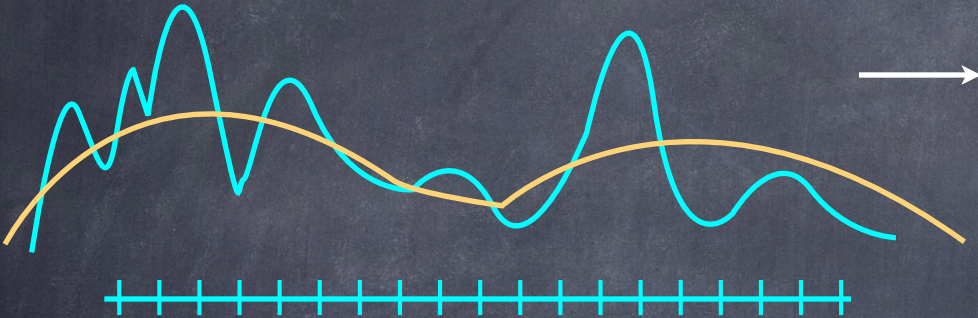




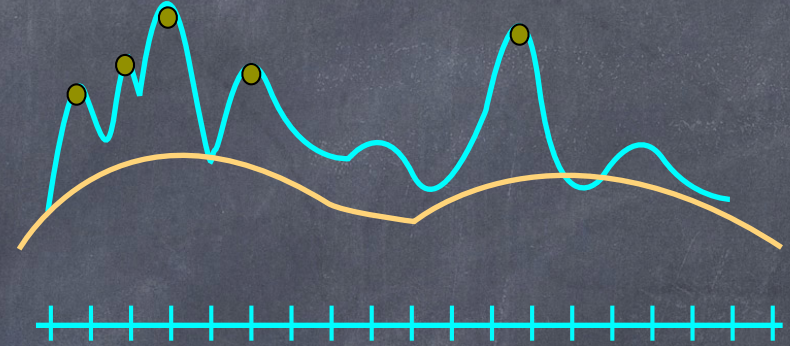
# Scale-dependent bias

## Prescription for calculating the halo bias

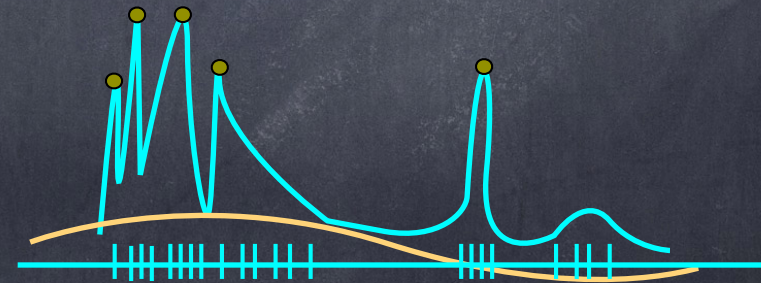
initial density field



initial proto-halo distribution



late time halo distribution

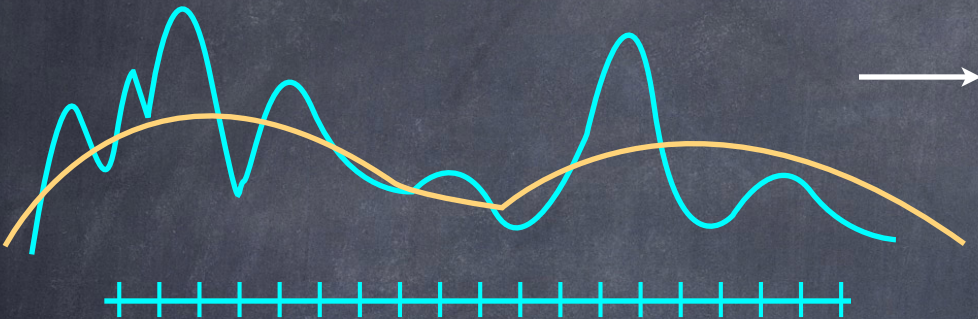




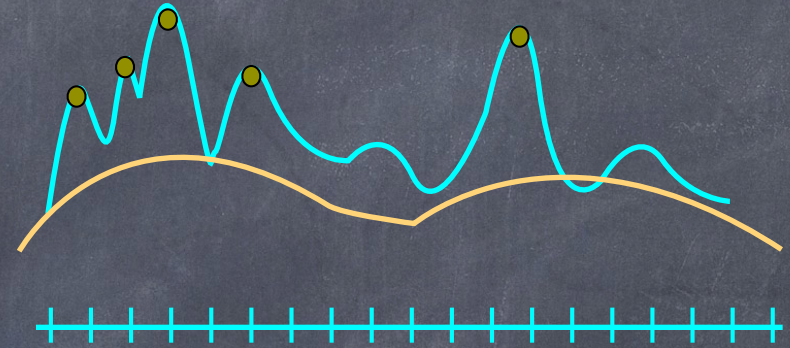
# Scale-dependent bias

## Prescription for calculating the halo bias

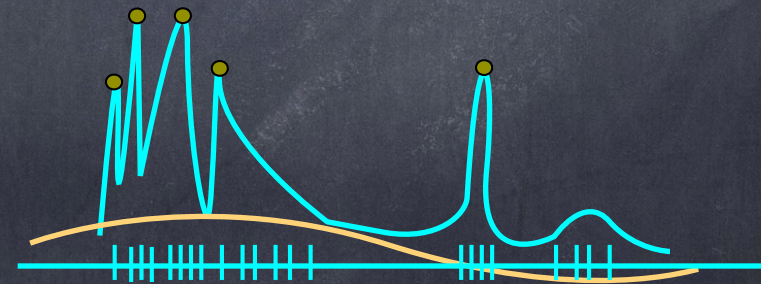
initial density field



initial proto-halo distribution



late time halo distribution



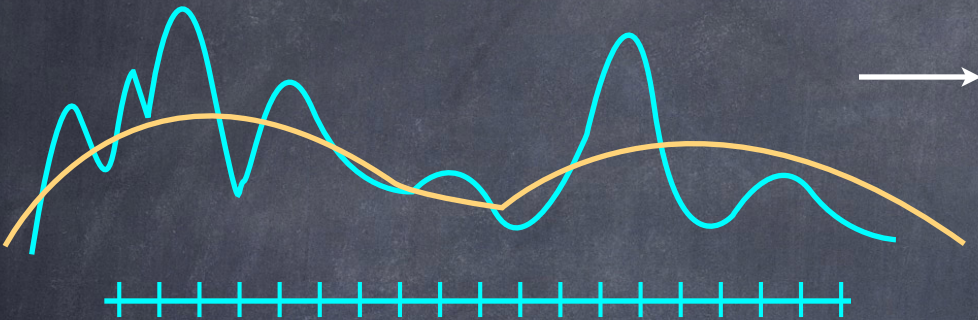
$$\frac{\delta n}{n} \equiv b \frac{\delta \rho}{\rho} \Big|_{\text{long-wavelength}}$$



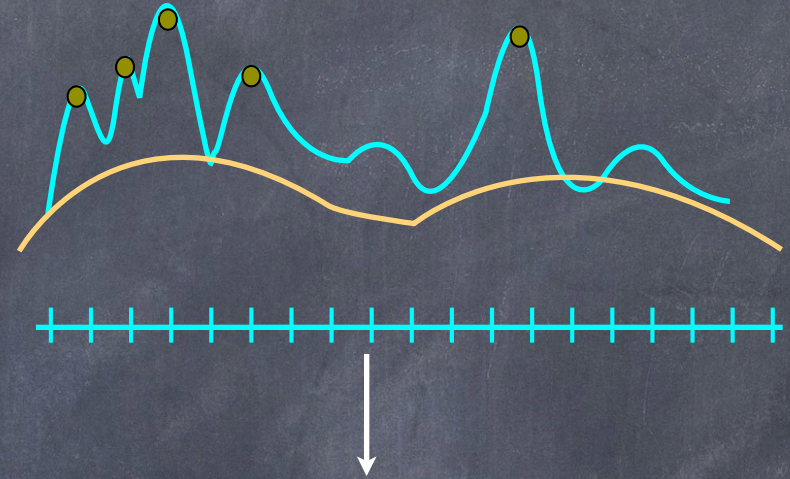
# Scale-dependent bias

## Prescription for calculating the halo bias

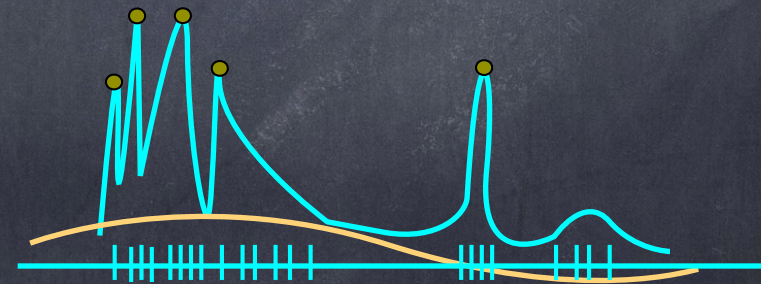
initial density field



initial proto-halo distribution



late time halo distribution



$$\frac{\delta n}{n} \equiv \left( b \frac{\delta \rho}{\rho} \right)_{\text{long-wavelength}}$$

want this!

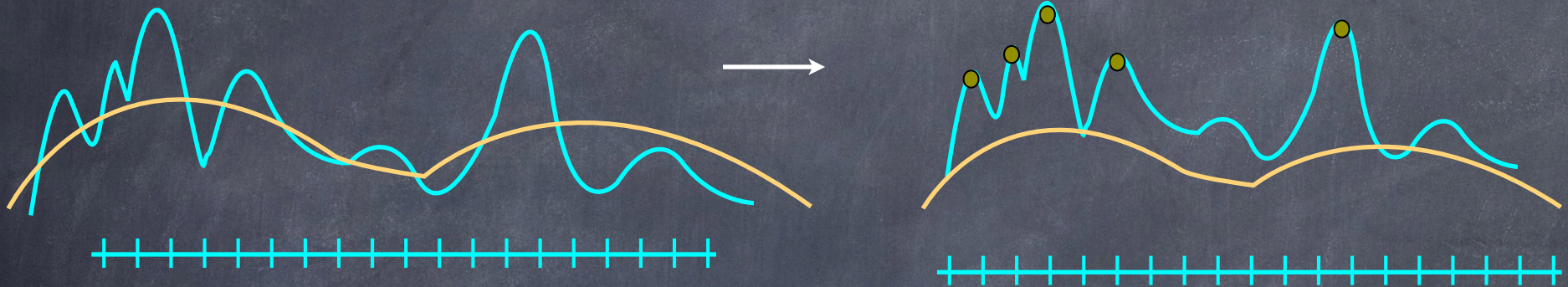


# Scale-dependent bias

## Prescription for calculating the halo bias

initial density field

initial proto-halo distribution



(i) In this step, the scale-dependent evolution of density perturbations causes

$$\frac{\delta n_{\text{Lagrangian}}(k)}{n} = b_{\text{Lagrangian}}(k) \frac{\delta \rho_{\text{cdm}}}{\rho_{\text{cdm}}}(k)$$



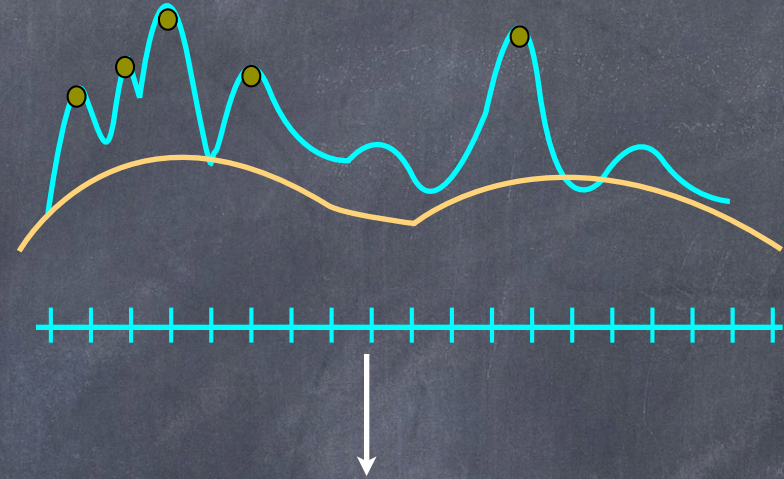
# Scale-dependent bias

## Prescription for calculating the halo bias

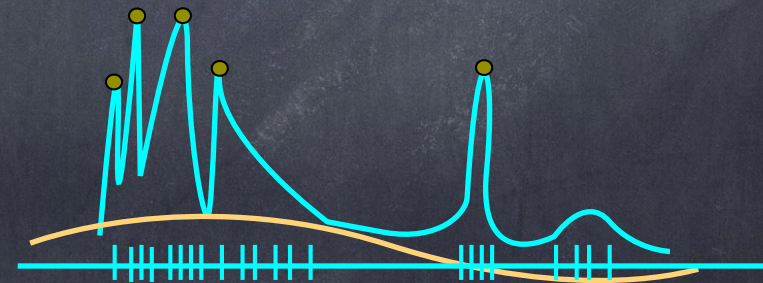
(ii) In this step, the free streaming of neutrinos causes

$$b(k) = \frac{\langle \delta_n(k) \delta_m(k) \rangle}{\langle \delta_m(k) \delta_m(k) \rangle}$$
$$= (1 + b_{\text{Lagrangian}}(k)) \frac{\langle \delta_{\text{cdm}}(k) \delta_m(k) \rangle}{\langle \delta_m(k) \delta_m(k) \rangle}$$

initial proto-halo distribution



late time **halo** distribution





# Scale-dependent bias

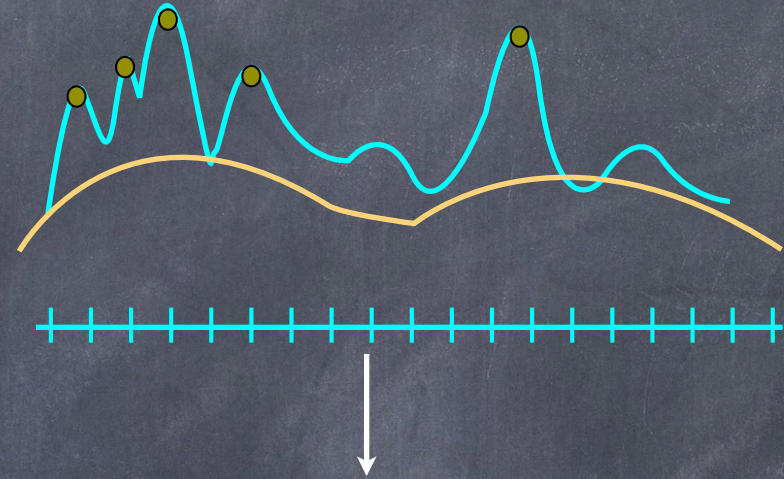
## Prescription for calculating the halo bias

(ii) In this step, the free streaming of neutrinos causes

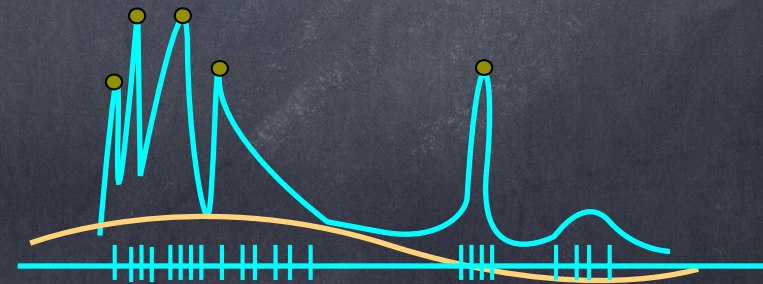
$$b(k) = \frac{\langle \delta_n(k) \delta_m(k) \rangle}{\langle \delta_m(k) \delta_m(k) \rangle}$$
$$= (1 + b_{\text{Lagrangian}}(k)) \frac{\langle \delta_{\text{cdm}}(k) \delta_m(k) \rangle}{\langle \delta_m(k) \delta_m(k) \rangle}$$

(i.e. halos trace CDM  $\rightarrow$  bias w.r.t total matter is scale-dependent)

initial proto-halo distribution



late time **halo** distribution





# Scale-dependent bias

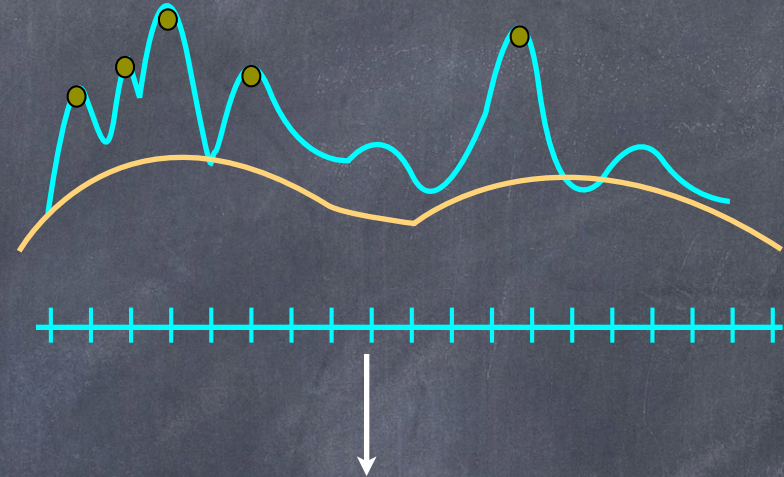
## Prescription for calculating the halo bias

(ii) In this step, the free streaming of neutrinos causes

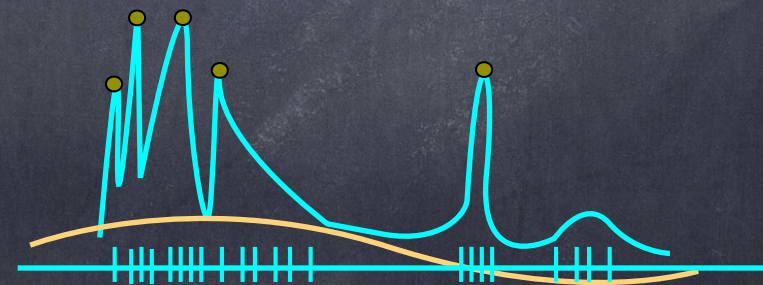
$$b(k) = \frac{\langle \delta_n(k) \delta_m(k) \rangle}{\langle \delta_m(k) \delta_m(k) \rangle}$$
$$= (1 + b_{\text{Lagrangian}}(k)) \frac{\langle \delta_{\text{cdm}}(k) \delta_m(k) \rangle}{\langle \delta_m(k) \delta_m(k) \rangle}$$

(i.e. halos trace CDM  $\rightarrow$  bias w.r.t total matter is scale-dependent)

initial proto-halo distribution



late time **halo** distribution



see also Villaescusa-Navarro, Marulli, Viel, Branchini, Castorina 2013  
Castorina, Sefusatti, Sheth, Villaescusa-Navarro, Viel 2014  
Biagetti, Desjacques, Kehagias, Riotto 2014



# Scale-dependent bias

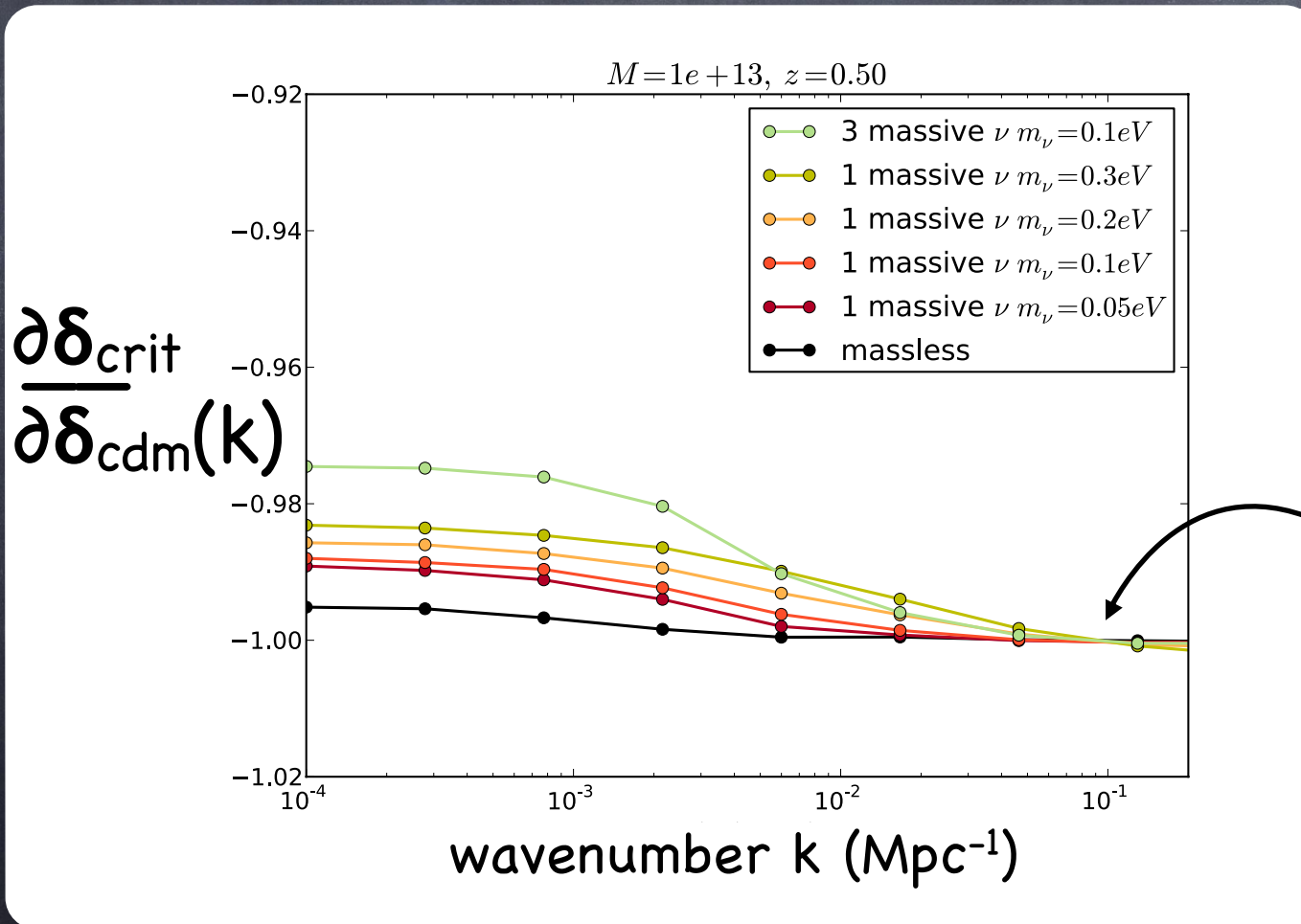
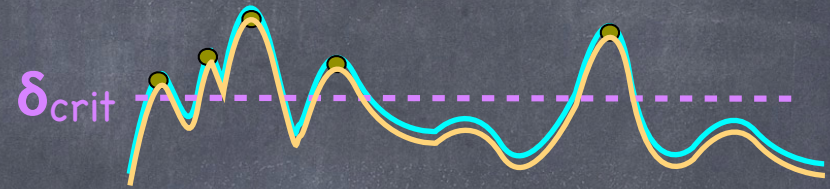
Numerical estimates for scale-  
dependent halo bias



# Scale-dependent bias

## Numerical results for halo bias

Scale-dependent changes to  $\delta_{\text{crit}}$



$$\delta_{\text{crit}} = \delta_{\text{crit}} - \delta_{\text{cdm}}(k)$$

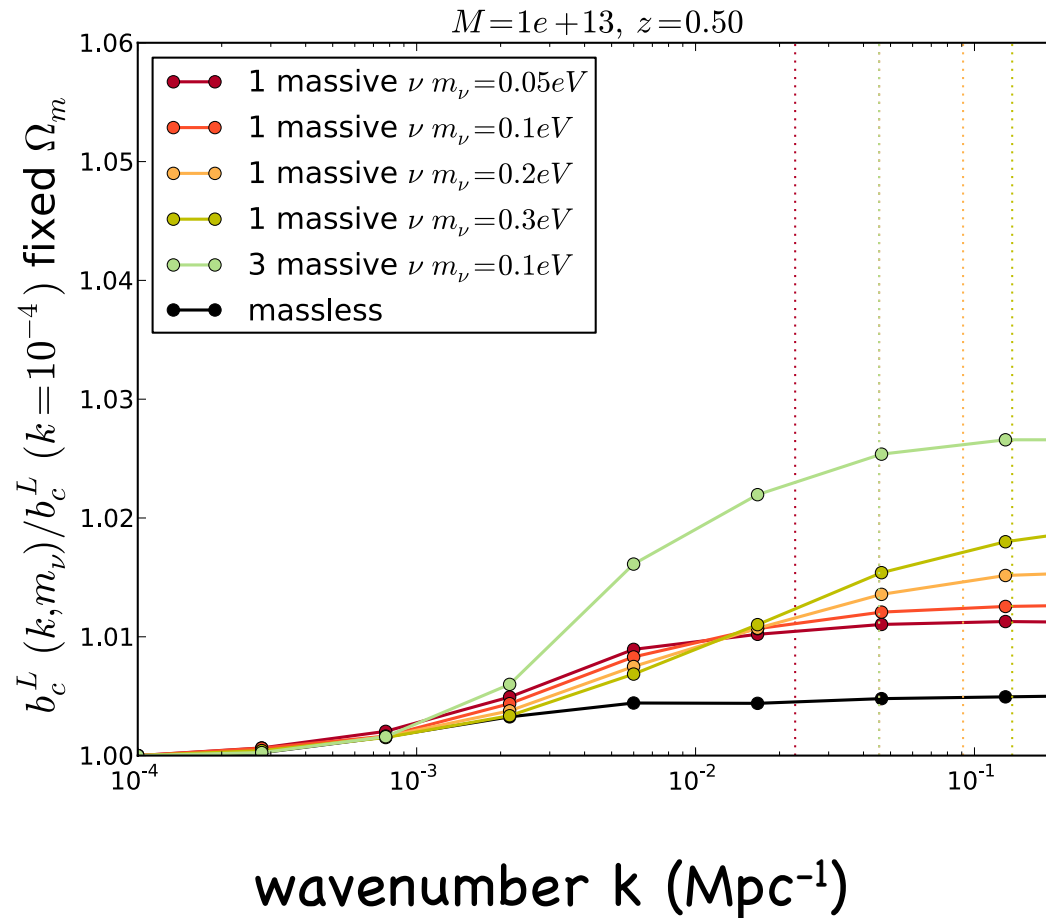


# Scale-dependent bias

## Numerical results for halo bias

scale-dependent  
change to

$$\delta n(k) = \frac{\partial n}{\partial \delta_{\text{crit}}} \frac{\partial \delta_{\text{crit}}}{\partial \delta_{\text{cdm}}(k)} \delta_{\text{cdm}}(k)$$



(Use Bhattacharya  
et al 2011 for  
 $n(M|\delta_{\text{crit}})$ )



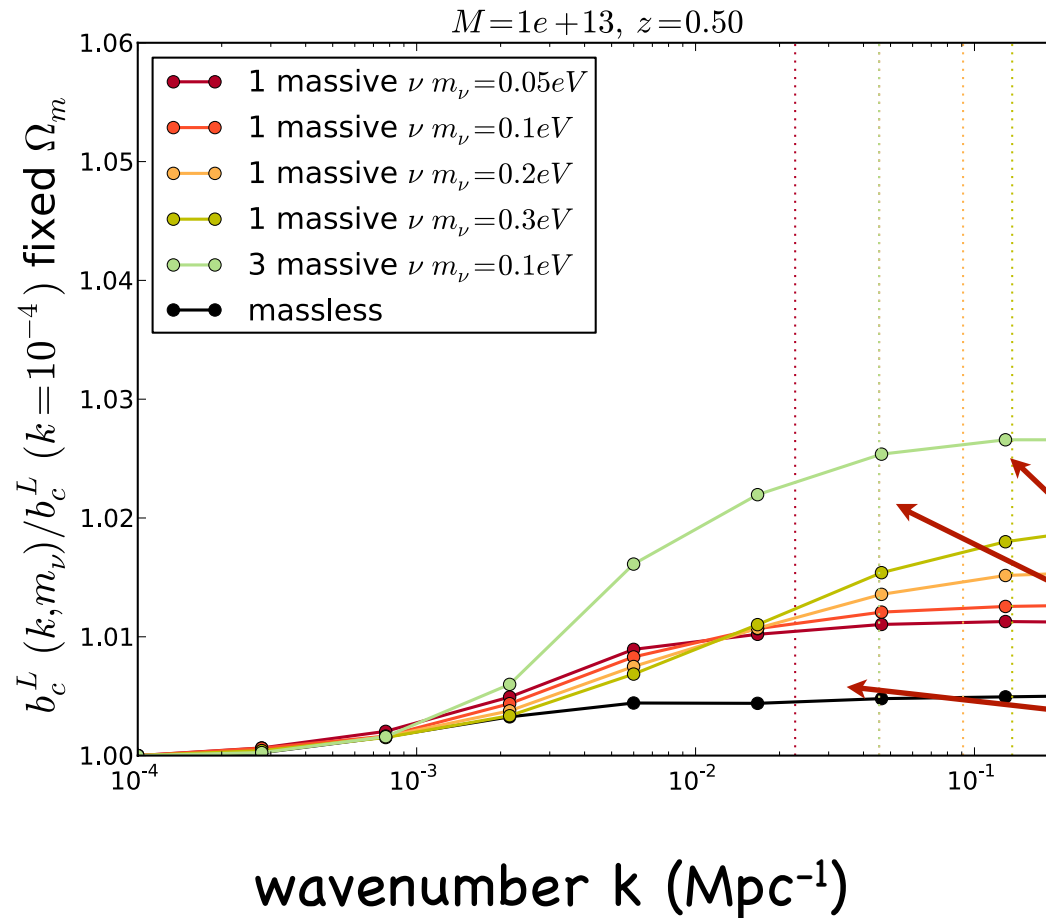
# Scale-dependent bias

## Numerical results for halo bias

scale-dependent  
change to

$$\delta n(k) = \frac{\partial n}{\partial \delta_{\text{crit}}} \frac{\partial \delta_{\text{crit}}}{\partial \delta_{\text{cdm}}(k)} \delta_{\text{cdm}}(k)$$

"Lagrangian halo bias"  $\equiv d \ln n / d \delta_{\text{cdm}}$



tiny step-  
like feature  
near the  
neutrino  
free-  
streaming  
scale

(Use Bhattacharya  
et al 2011 for  
 $n(M | \delta_{\text{crit}})$ )



# Scale-dependent bias

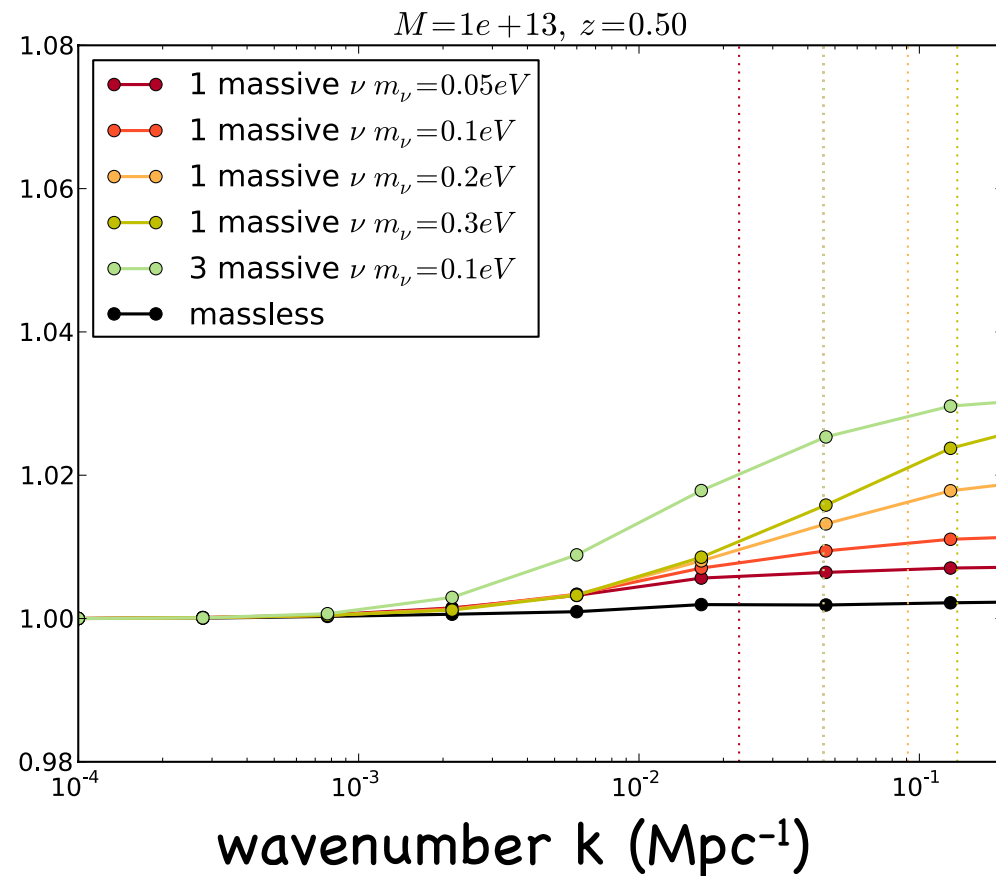
## Numerical results for halo bias

scale-dependent change  
to final bias

$$\delta n(k)/n = b(k) \delta_{\text{matter}}(k)$$

$$b(k) = \sqrt{P_{\text{hh}}(k)/P_{\text{mm}}(k)}$$

fractional change in Eulerian halo bias



(Use Bhattacharya  
et al 2011 for  
 $n(M) \delta_{\text{crit}}$ )

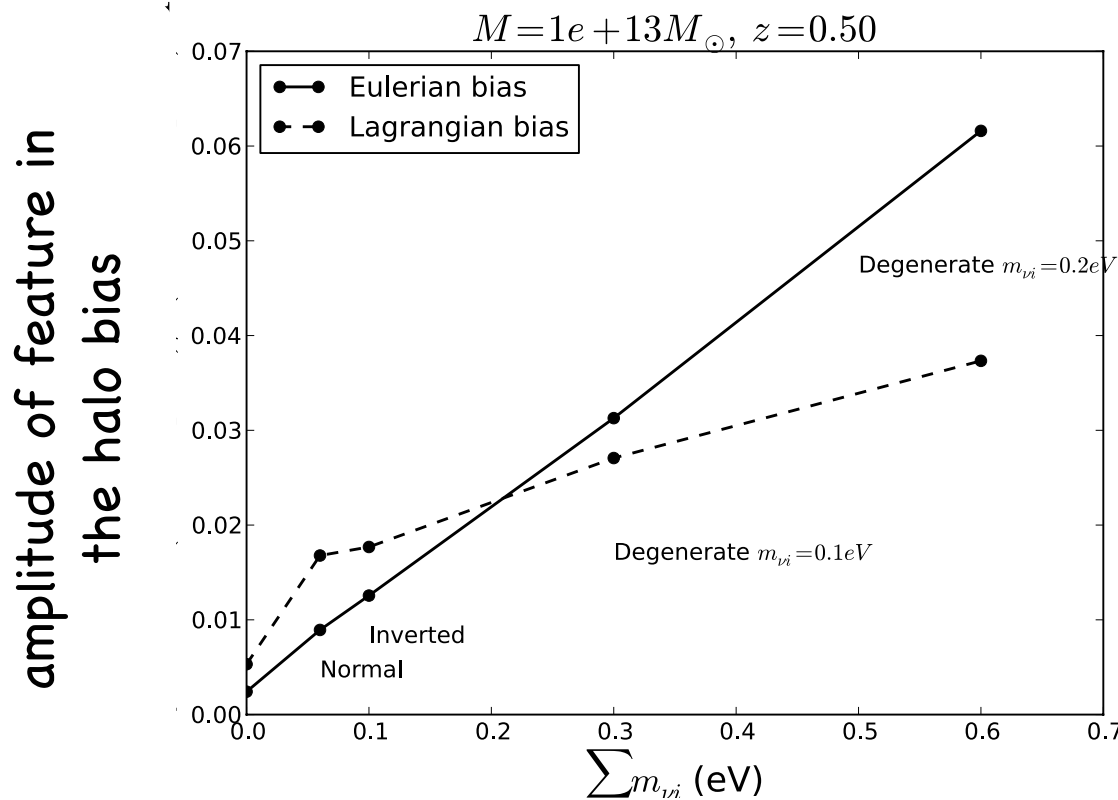


# Scale-dependent bias

## Numerical results for halo bias

scale-dependent change  
to final bias

$$\delta n(k)/n = b(k) \delta_{\text{matter}}(k)$$



(Use Bhattacharya  
et al 2011 for  
 $n(M) \delta_{\text{crit}}$ )

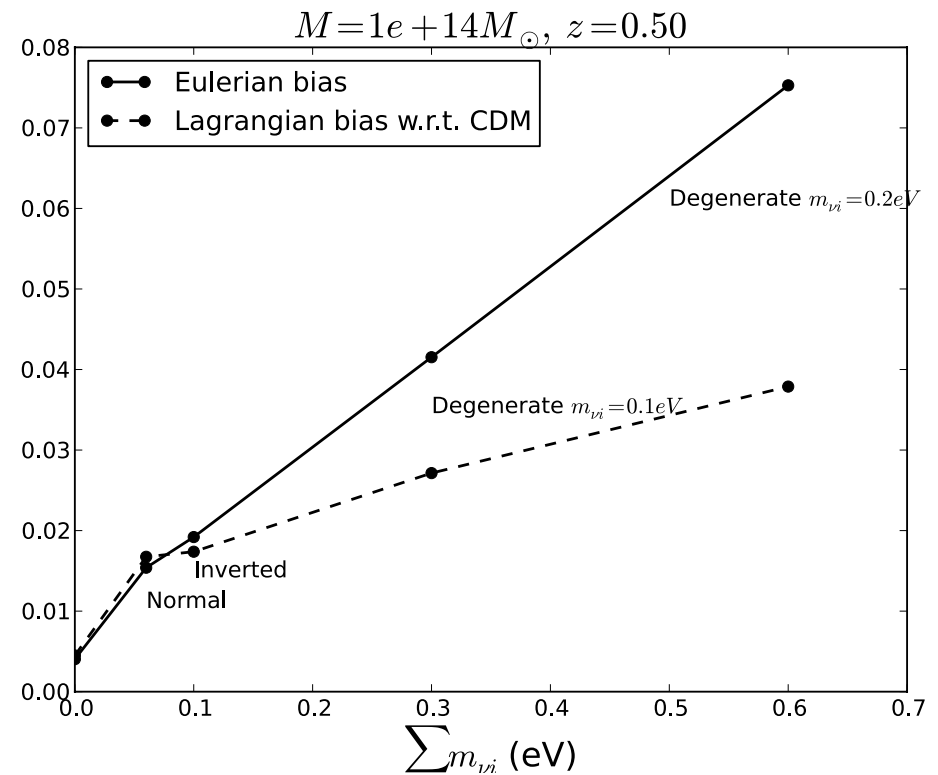
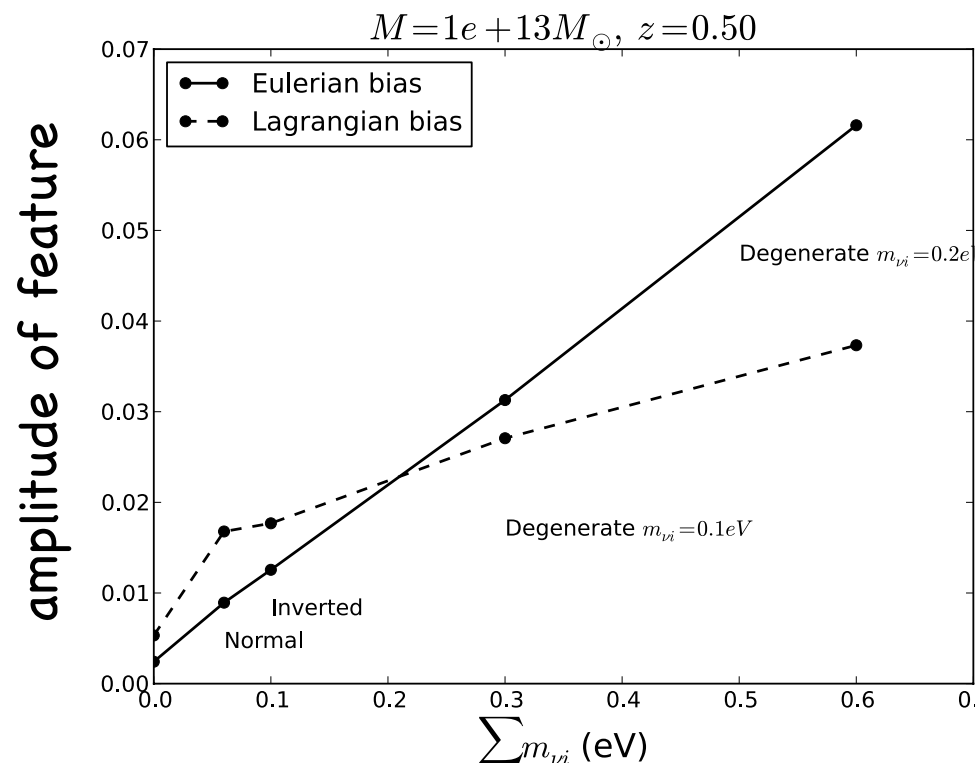


# Scale-dependent bias

## Numerical results for halo bias

scale-dependent change  
to final bias

$$\delta n(k)/n = b(k) \delta_{\text{matter}}(k)$$





Scale-dependent bias

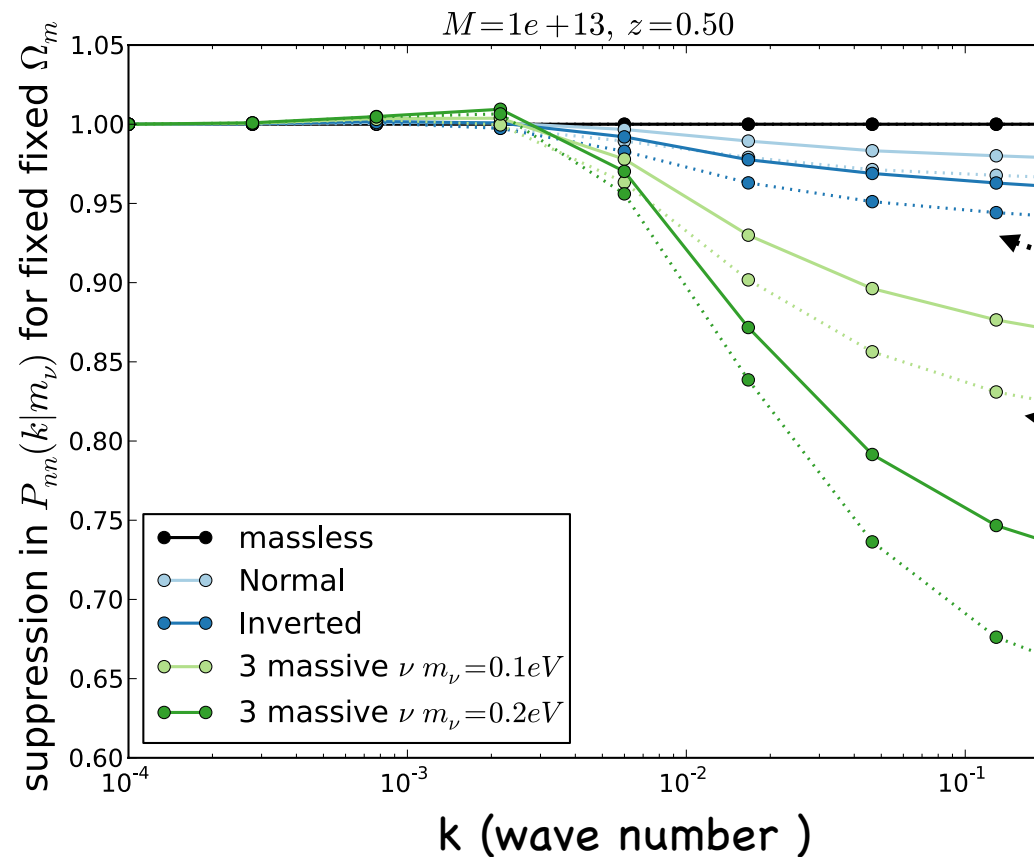
Observational  
consequences of scale-  
dependent bias?



# Observational consequences of scale dependent bias?

matter power spectrum, or (incorrectly) assuming constant bias

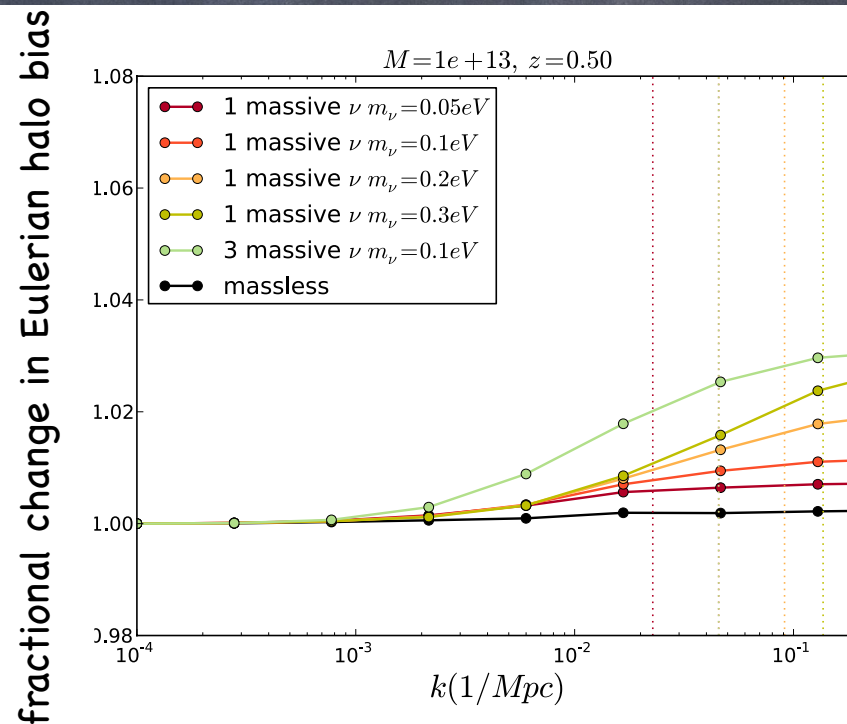
suppression in  
galaxy power  
spectrum less  
than in matter  
power spectrum





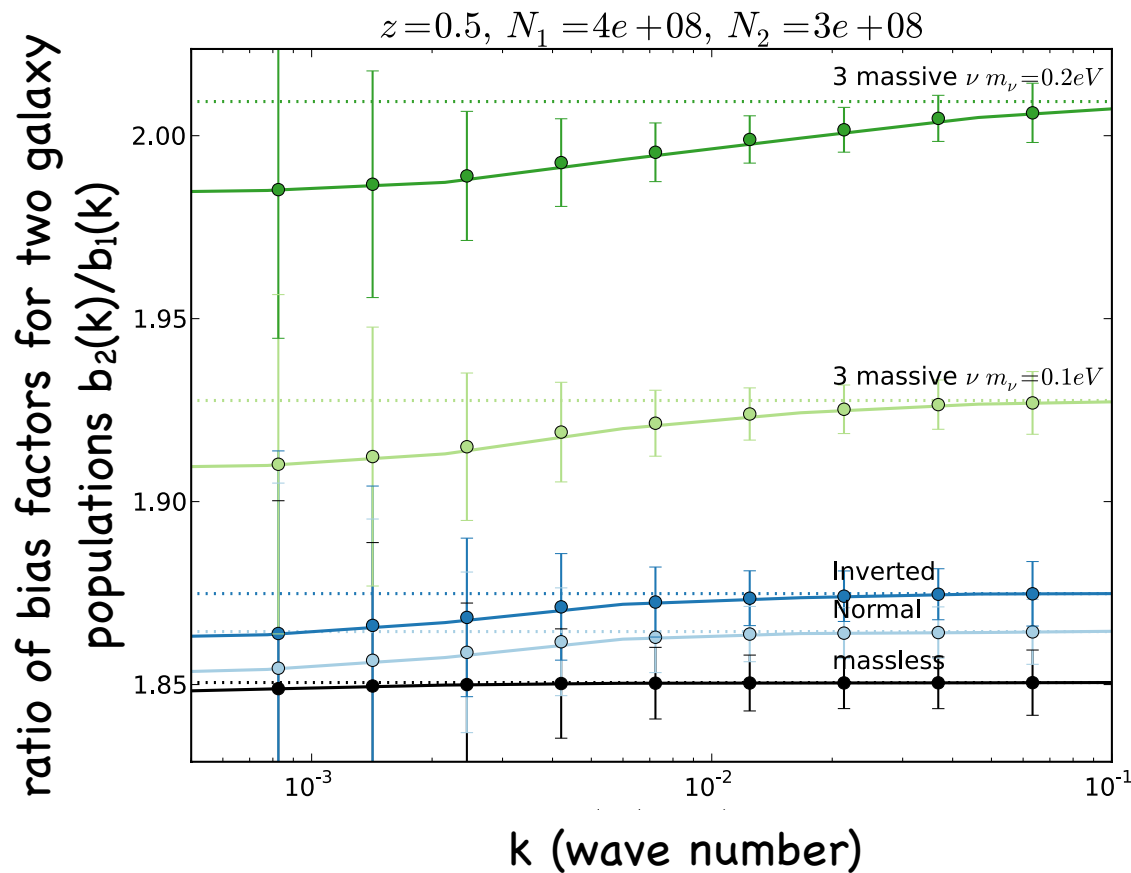
# Scale-dependent bias

But the scale-dependent halo bias is itself an observable!





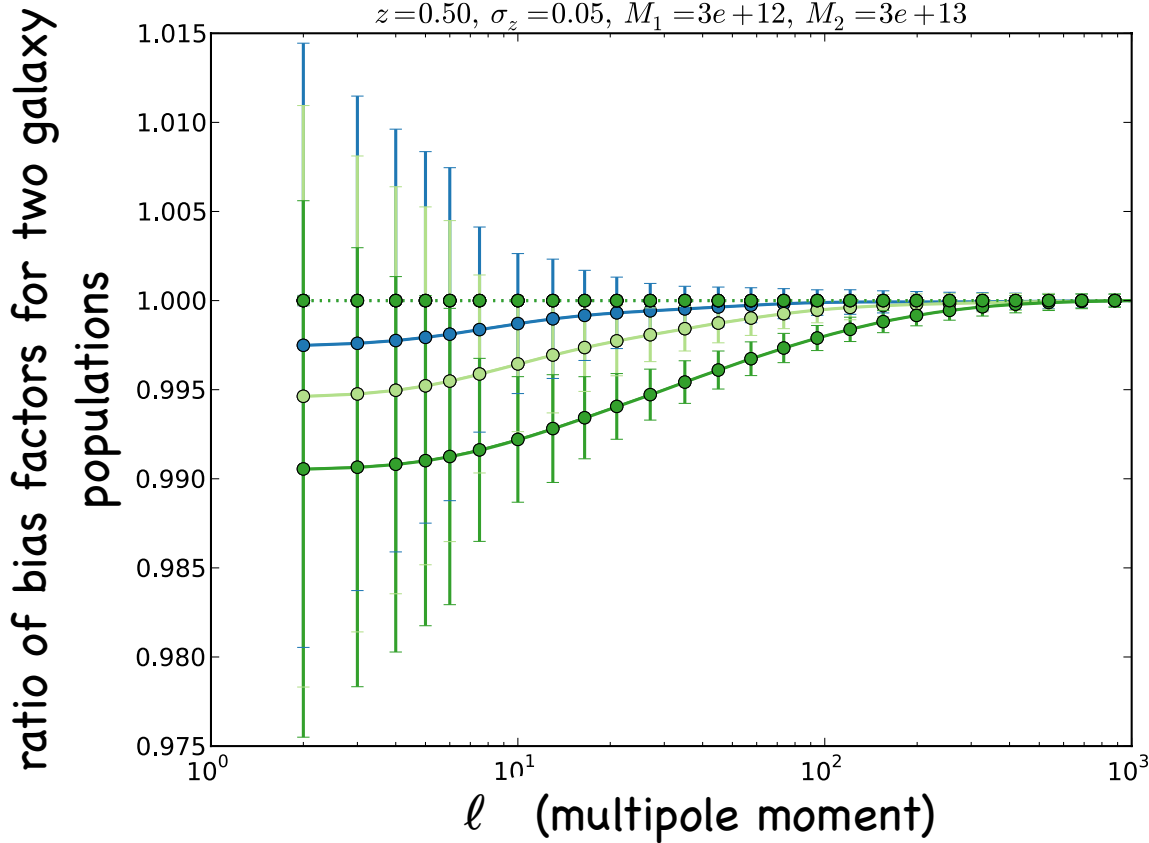
# The scale-dependent halo bias is an observable!



$$\sigma_{b1/b2} \sim \frac{1}{\sqrt{n_1 P_{g2g2}}}$$



# The scale-dependent halo bias is an observable!



$$\sigma_{b1/b2} \sim \frac{1}{\sqrt{N_\ell} n_1 C_{g2g2}}$$



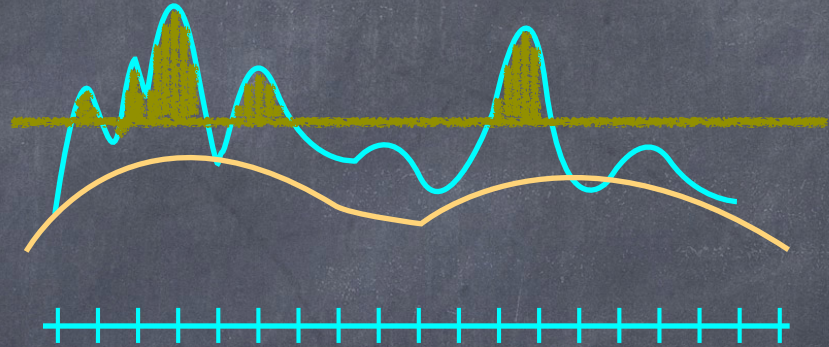
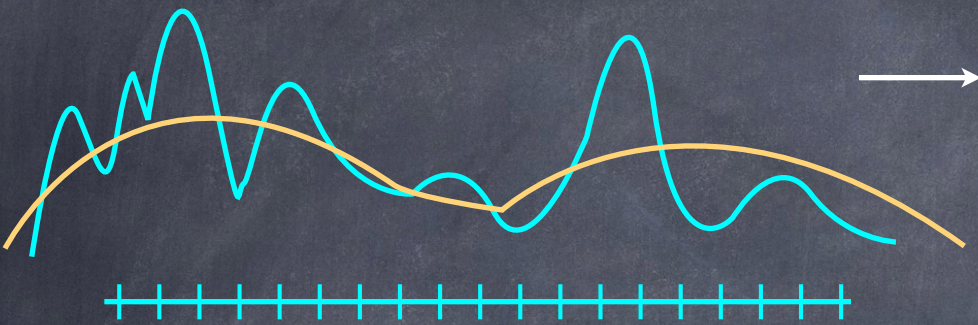
Fewer massive halos  
from massive neutrinos



# Fewer massive halos

initial density field

mass that collapses into halos

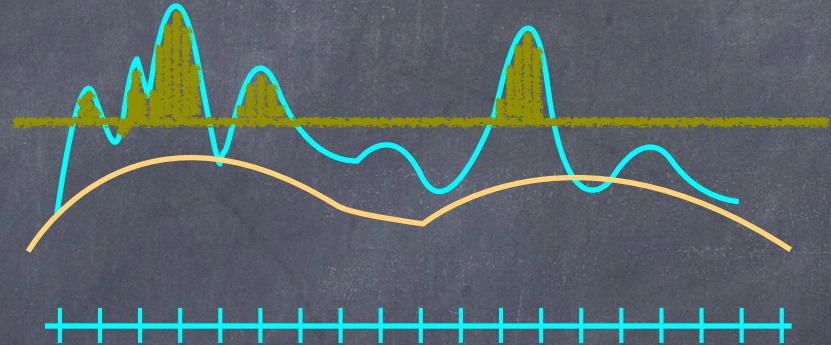
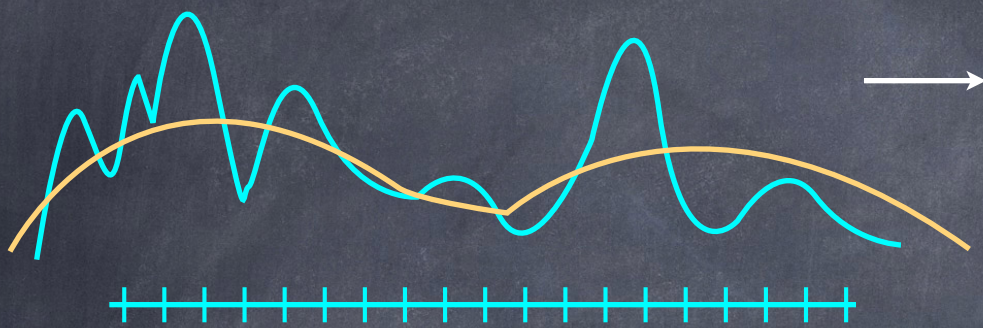




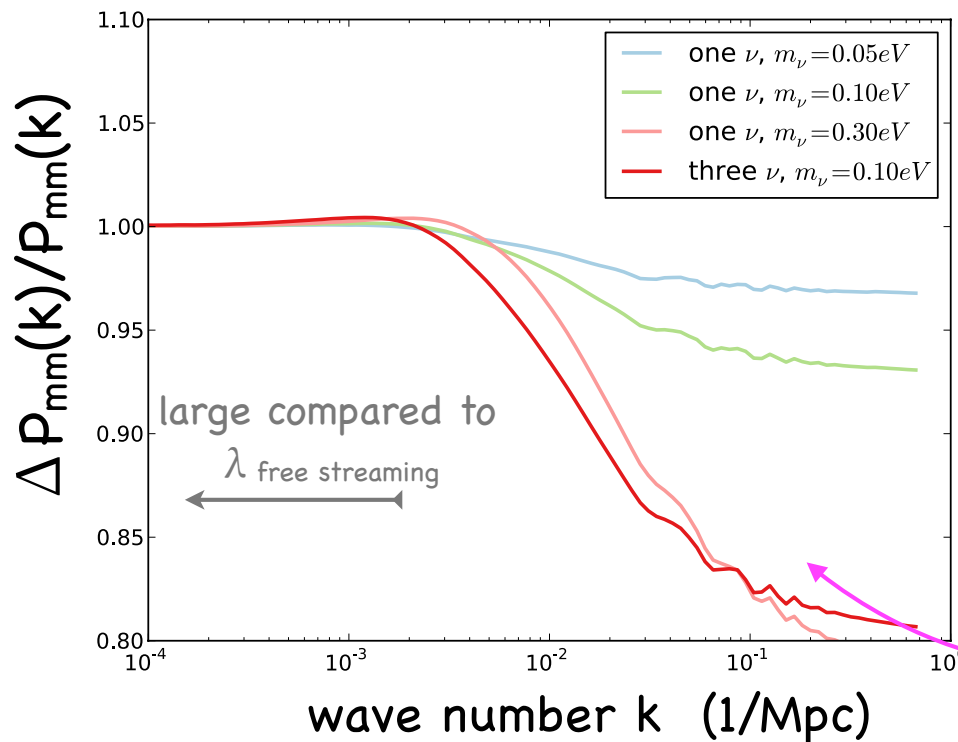
# Fewer massive halos

initial density field

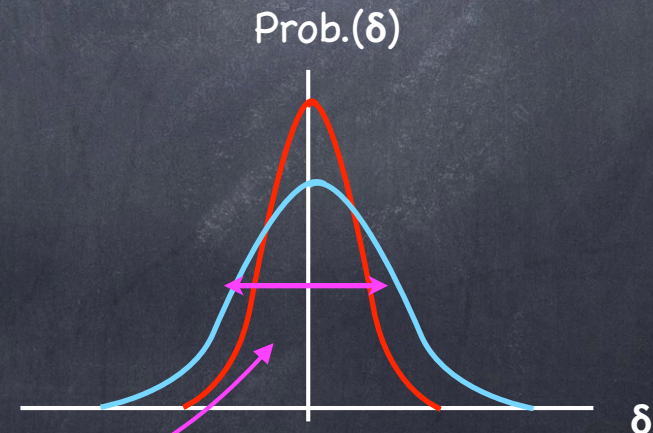
mass that collapses into halos



change in typical amplitude of  $\delta_m(k)$  from  $m_\nu \neq 0$



Fewer large-amplitude density fluctuations

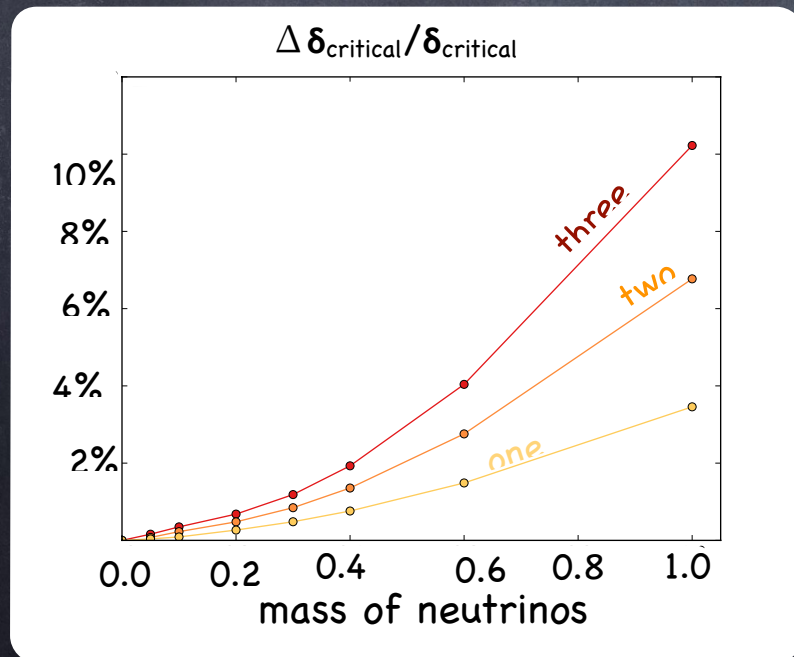
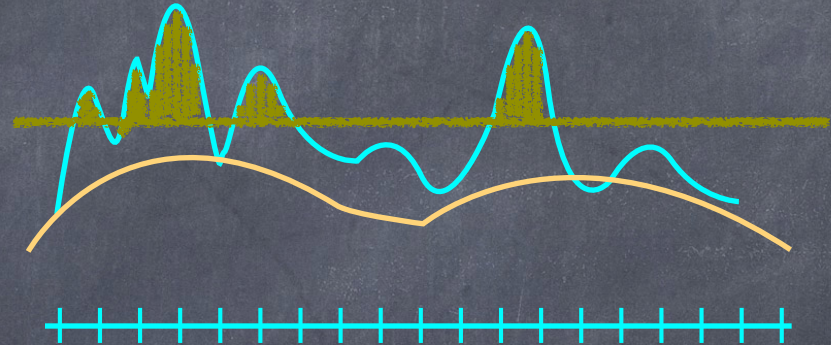
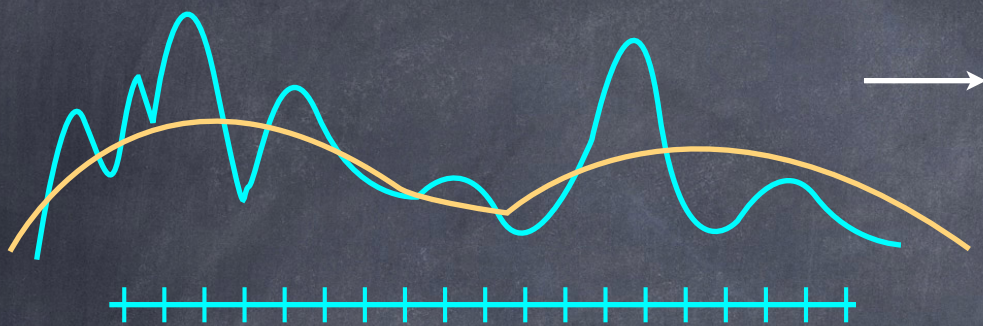




# Fewer massive halos

initial density field

mass that collapses into halos



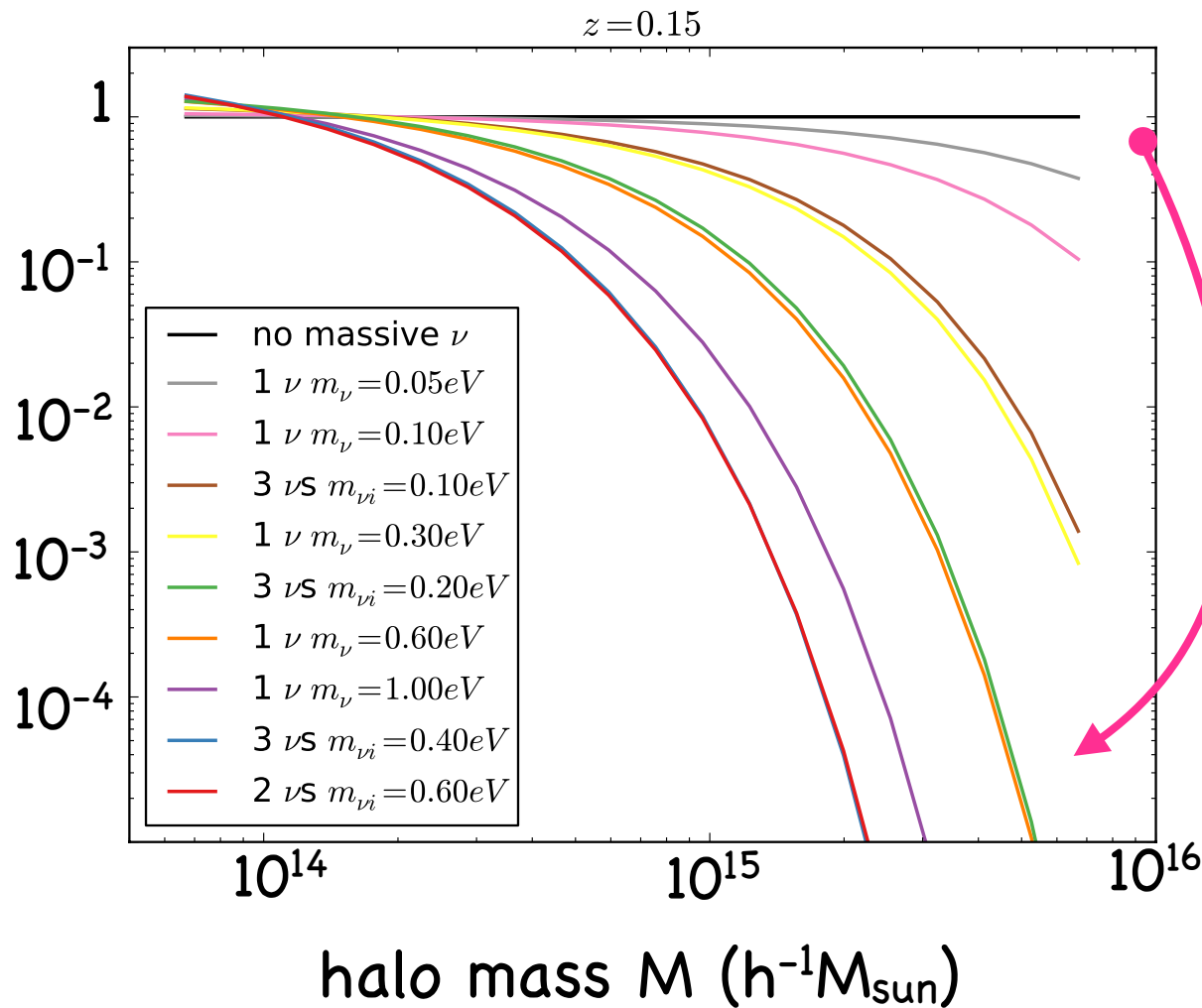
And, higher threshold density to form a halo



# Fewer massive halos

Many fewer massive halos

suppression in halo abundance



increasing  
 $m_\nu$  and/or  
 $n_\nu$

using Bhattacharya et al fitting formula for  $n(M)$  with our  $\delta_{\text{crit}}$

(changes w.r.t. model w same  $\Omega_m$  but  $\Omega_\nu = 0$ )

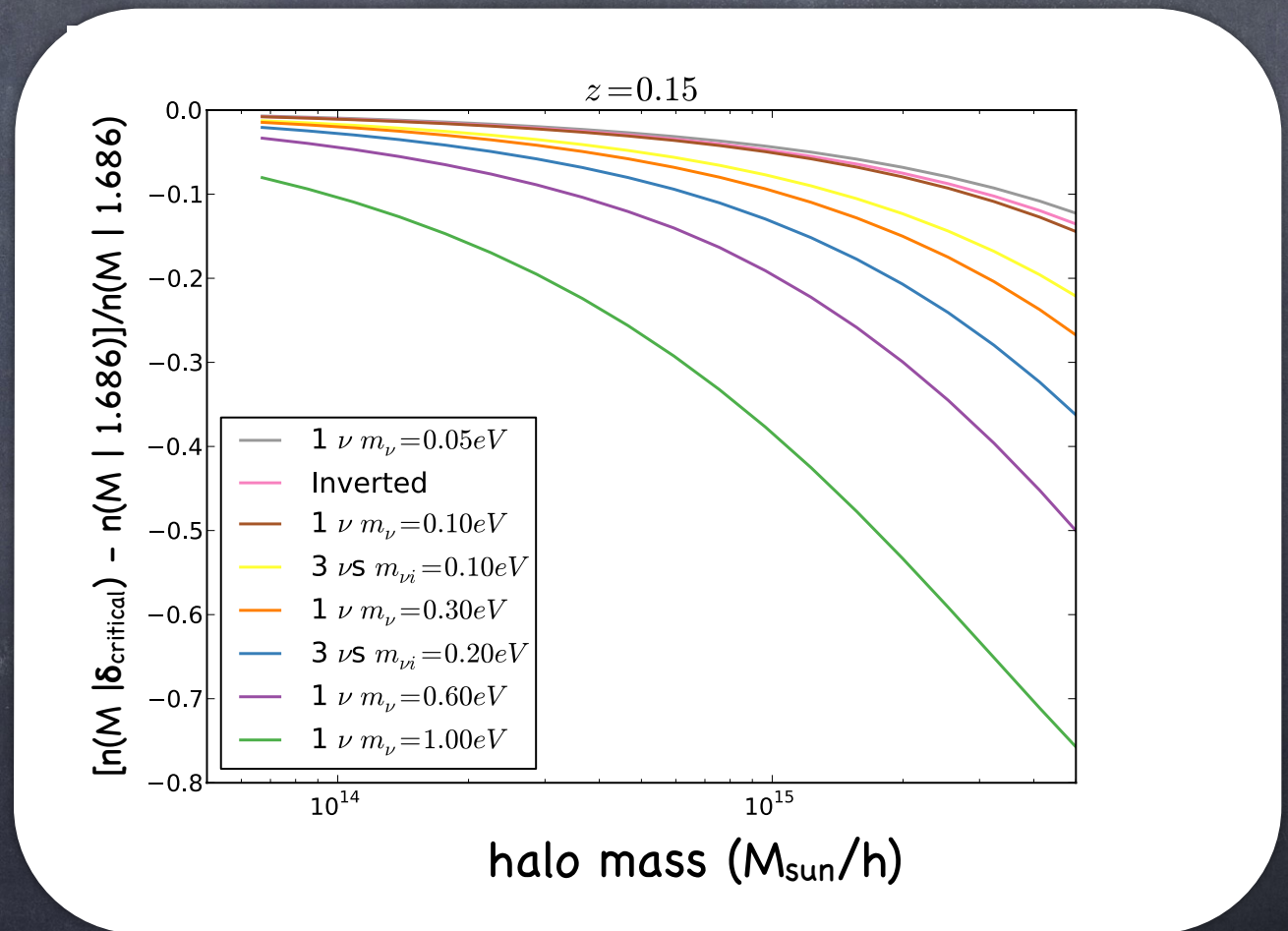
Bhattacharya, Heitmann, White, Lukic, Wagner, 2011  
ML 2014



# Fewer massive halos



Many fewer massive halos



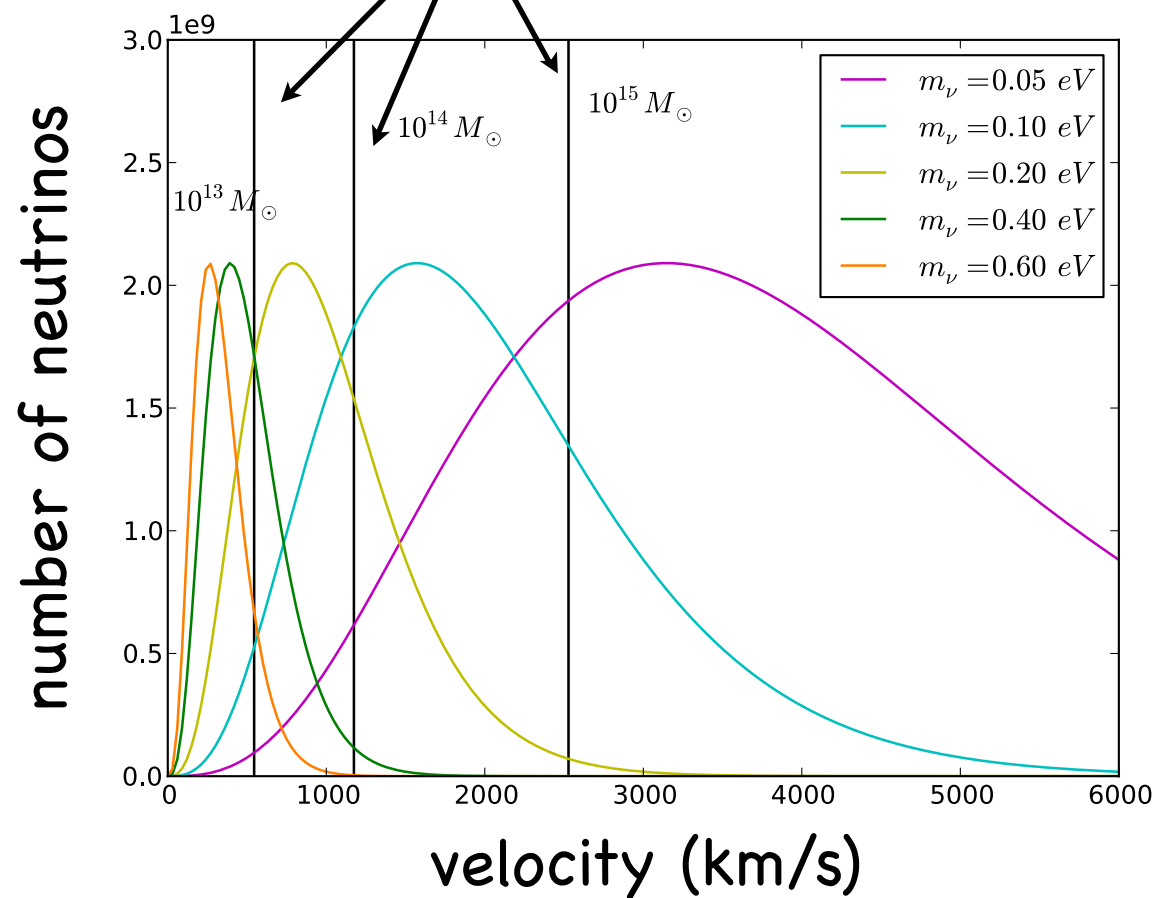


Neutrinos accrete onto  
these cold dark matter  
halos



# Neutrino Accretion

escape velocity of dark matter halos

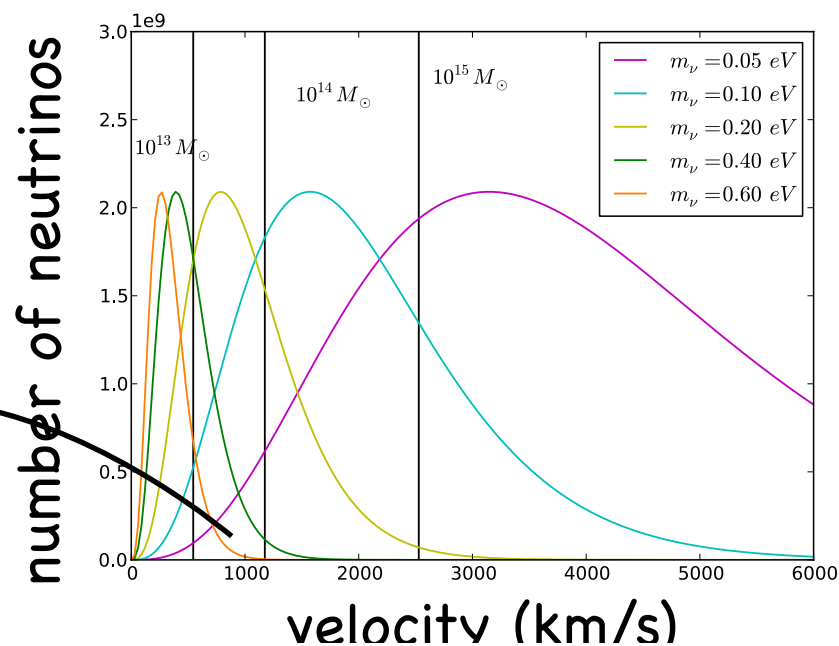
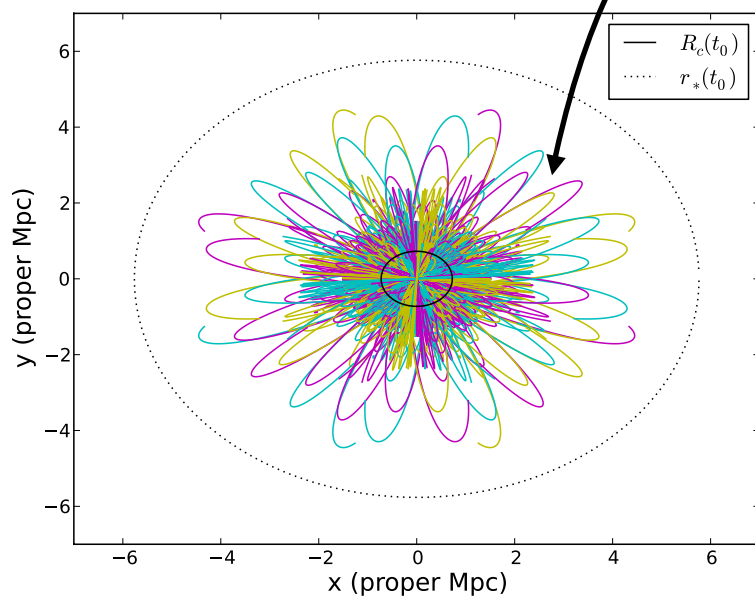




# Neutrino Accretion

low velocity  
neutrinos end  
up bound in  
halos

shown are  $m_\nu = 0.05 \text{ eV}$  neutrinos  
around  $M = 10^{14} M_{\text{sun}}$  halo

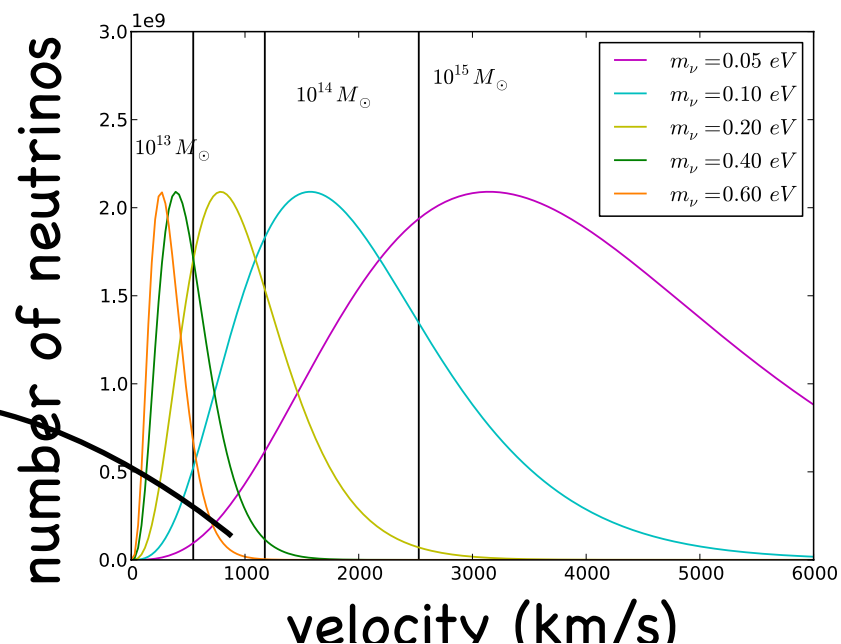
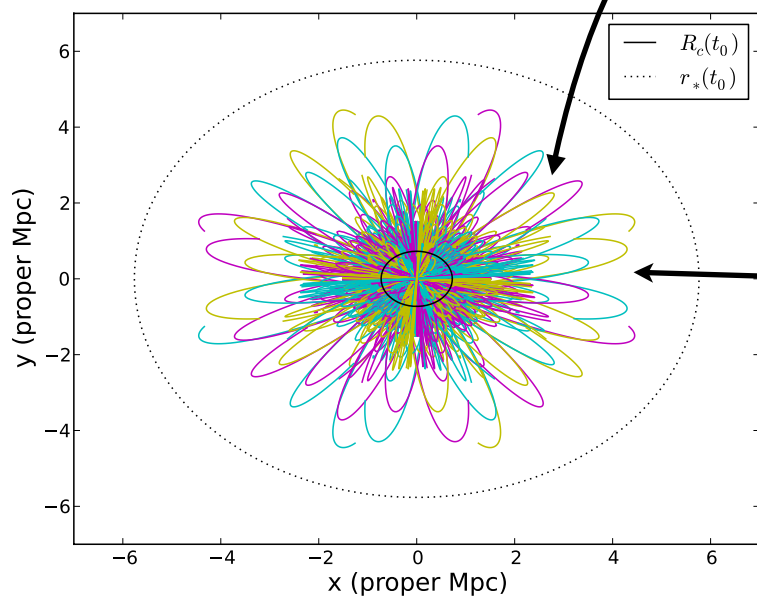




# Neutrino Accretion

low velocity  
neutrinos end  
up bound in  
halos

shown are  $m_\nu = 0.05 \text{ eV}$  neutrinos  
around  $M = 10^{14} M_{\text{sun}}$  halo

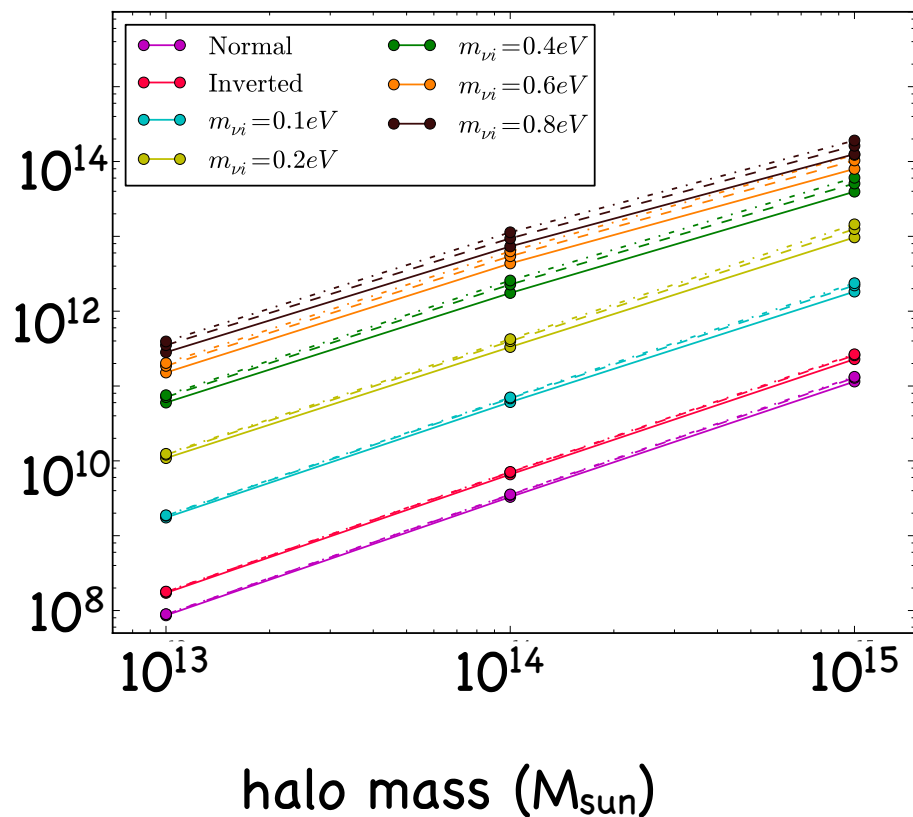


the accreted **neutrino**  
halo is puffy in  
comparison with the  
**CDM!**

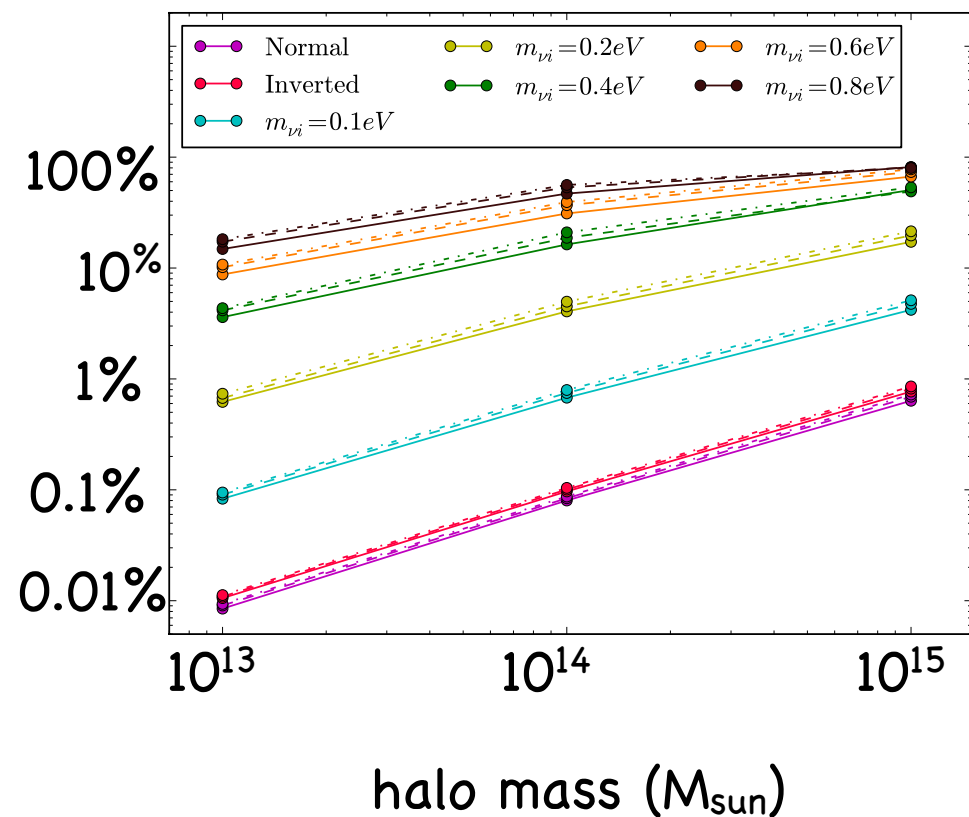


# Neutrino Accretion

neutrino mass around halo ( $M_{\text{sun}}$ )



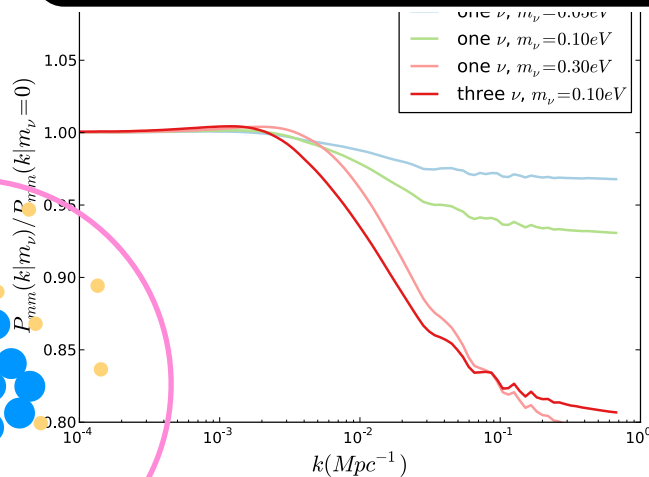
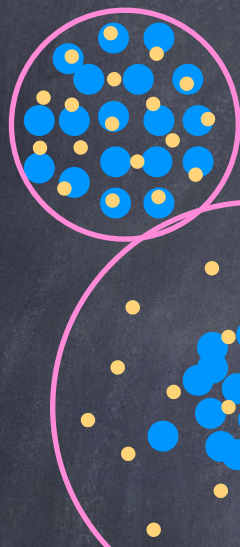
fraction that's bound to the halo



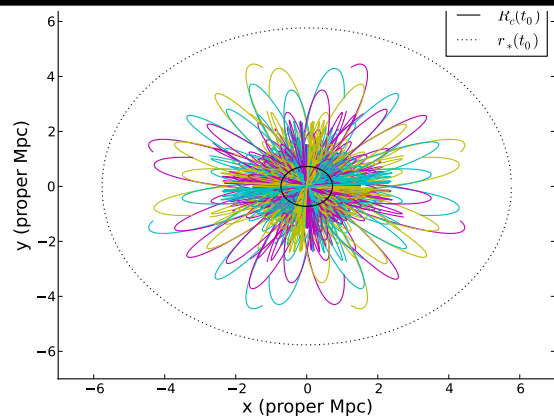


# Neutrino Effects in Large-scale Structure

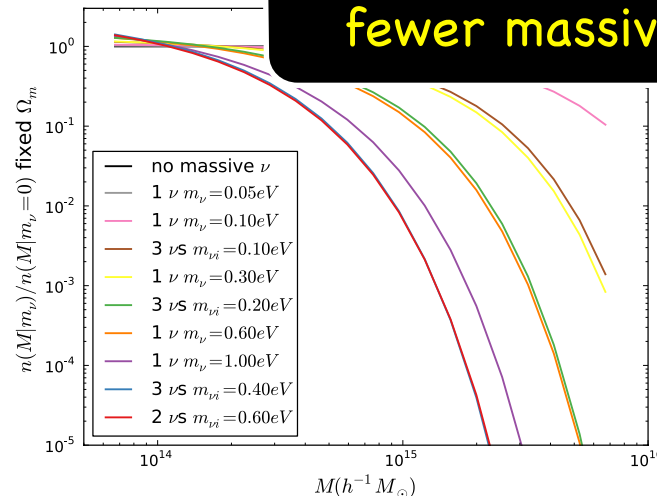
less power in small-scale density fluctuations



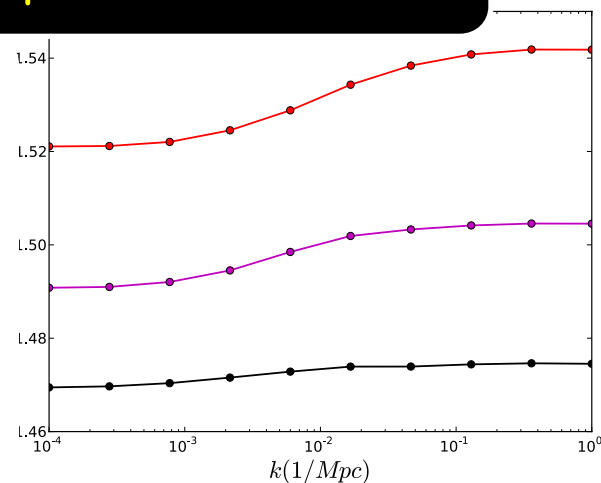
puffy neutrino halos around CDM halos



fewer massive halos



scale-dependent halo bias





# Accuracy of these predictions?

N-body simulations are the community standard for cold dark matter structure.

## Simulations with massive neutrinos?

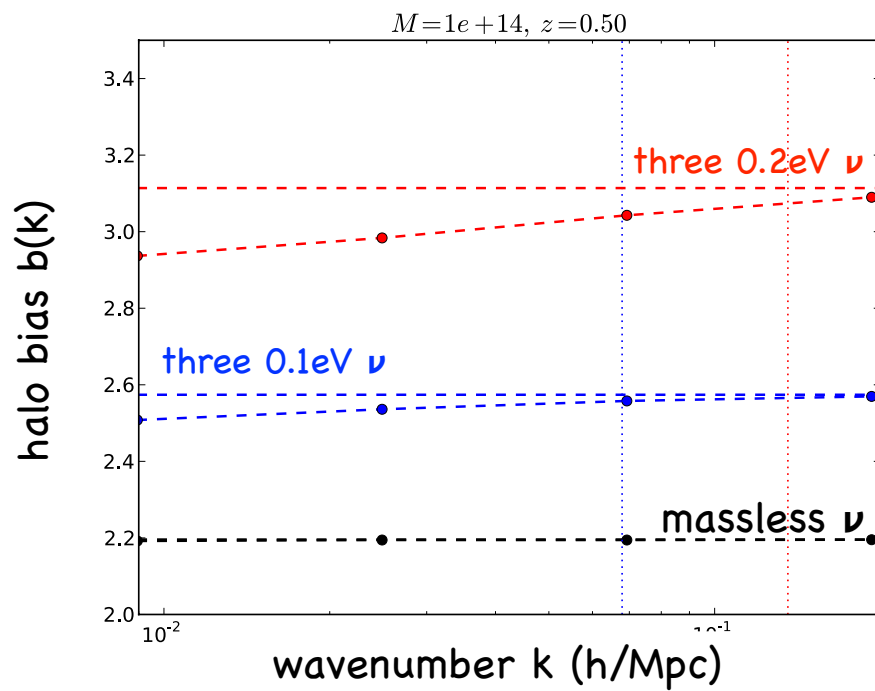
- (i) Tricky. very few exist, very new
- (ii) Want a model that provides insight into the physical processes responsible for new effects
- (iii) Don't want to rerun for every possible neutrino mass hierarchy scenario
- (iv) It will be great to make comparisons in the future!



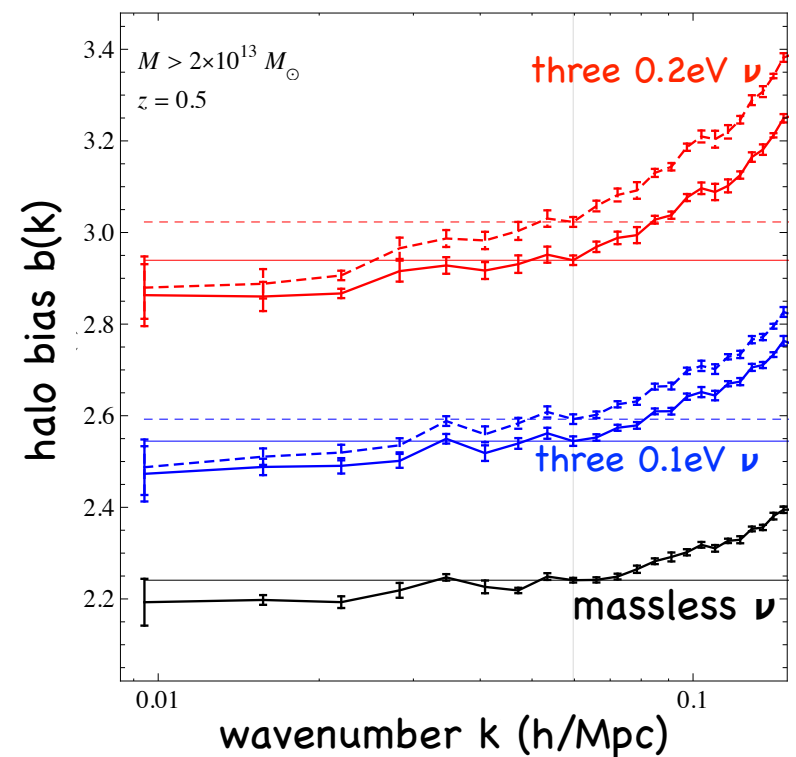
# Scale-dependent bias from massive neutrinos

comparison with sims looks reasonable!

my calculations



simulations from Castorina et al 2013





# Conclusions

- Cosmology provides interesting information about neutrinos!
- Scale-dependent halo bias is a **new signal** of massive neutrinos in large-scale structure
- Scale-dependent halo bias is a **new systematic** for massive neutrinos in large-scale structure
- Neutrinos decrease abundance of halos — Need to be careful with predictions for  $m_\nu \geq 0.3\text{eV}$ !
- Eventually neutrinos accrete onto very massive halos!